

SSNV133 - Uniaxial traction and compression. Mixed work hardening

Summary:

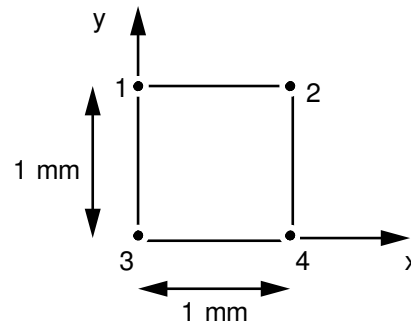
The purpose of this test is to validate the elastoplastic behaviors `VMIS_ECMI_TRAC` and `VMIS_ECMI_LINE`, which combines an isotropic work hardening (linear or given by a traction diagram) and a linear kinematic work hardening.

The geometrical and mechanical data make it possible to be in uniaxial situation (uniform constraints, only one nonworthless component). The reference solution is simple, analytical. This test simply makes it possible to check that the integration of the model of behavior is correct.

3 modelings make it possible to check the uniaxiality of the constraints: `3D`, `AXIS`, `C_PLAN`.

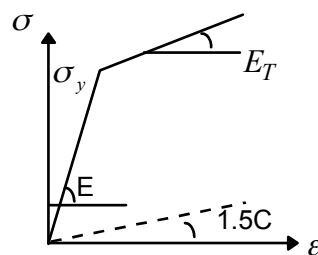
1 Problem of reference

1.1 Geometry



1.2 Material properties

Elastoplastic law of behaviour to mixed work hardening (isotropic linear and kinematic linear).



$$\begin{aligned}
 C &= 20000 \text{ MPa} \\
 E &= 200000 \text{ MPa} \\
 \nu &= 0.3 \\
 \sigma^Y &= 400 \text{ MPa} \\
 E_T &= 40000 \text{ MPa}
 \end{aligned}$$

1.3 Boundary conditions and loadings

The plate is blocked according to O_y along the side [3.4], following O_x along the side [1.3] while being subjected to a displacement imposed in $y : u_y^D$ along the side [1.2].

The way of loading is the following:

| t | u_y^D (mm) |
|-----|--------------------|
| 1 | $2 \cdot 10^{-3}$ |
| 2 | $4.5d-3$ |
| 3 | $0.1d-3$ |
| 4 | $-2 \cdot 10^{-3}$ |

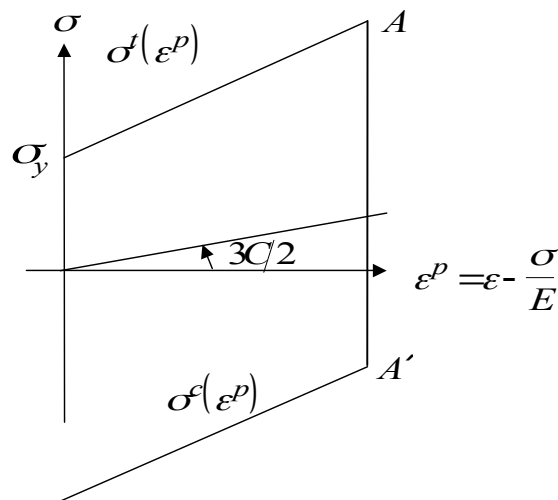
2 Reference solution

2.1 Method of calculating used for the reference solution

The reference solution is obtained by an analytical calculation.

Imposed displacement u_y^D provides the deformation immediately $\varepsilon_{yy} = \frac{u_y^D}{1}$. Only this component

(corresponding to the nonworthless component of the tensor of the constraints) interests us here. In addition, to calculate the behavior, it is necessary to extract from the data the isotropic function of work hardening $R(p)$:



$$\sigma^t = F(\varepsilon) = \sigma_y + \frac{E \cdot E_T}{E - E_T} p$$

$$R(p) = \sigma_y + \left[\frac{E \cdot E_T}{E - E_T} - \frac{3}{2} C \right] \cdot p$$

2.1.1 T = 1: elastic behavior

Indeed, the behavior is elastic until $t=1$. For $t=1$, $\sigma_{yy} = E\varepsilon_{yy} = 400 \text{ MPa}$ reached the threshold of plasticity just.

2.1.2 T = 2: elastoplastic load

When one reaches the criterion of plasticity (in load or discharge), one a:

$$\left| \sigma - \frac{3}{2} C \varepsilon^p \right| = R(p)$$

$$\sigma = E(\varepsilon - \varepsilon^p)$$

For the load, it is necessary to solve $\sigma^t = F(\varepsilon) = \sigma_y + \frac{E \cdot E_T}{E - E_T} p = \sigma_y + \frac{E \cdot E_T}{E - E_T} \left(\varepsilon - \frac{\sigma^t}{E} \right)$

what gives again: $\sigma^t = \sigma_y + E_T \left(\varepsilon - \frac{\sigma_y}{E} \right)$: one moves on the traction diagram up to point A such as:

$$\sigma_A^t = E \left(\varepsilon_A - \varepsilon_A^p \right)$$

2.1.3 T = 3: elastic discharge

The discharge is elastic up to the point A' :

$$- \sigma^{A'} + \frac{3}{2} C \varepsilon_A^p = R(p_A)$$

$$\sigma^{A'} = E \left(\varepsilon^{A'} - \varepsilon_A^p \right)$$

2.1.4 T = 4: elastoplastic load in compression

$$\sigma^c = \frac{3}{2} C \varepsilon^p - R(p)$$

2.2 Results of Reference

| t | u_y^D (mm) | σ_{yy} (MPa) |
|-----|--------------|---------------------|
| 1 | 2.10^{-3} | 400 |
| 2 | 4.5d-3 | 500 |
| 3 | 0.1d-3 | -380 |
| 4 | -2.10^{-3} | -464 |

2.3 Uncertainty on the solution

Analytical solution.

2.4 Bibliographic references

- Relation of behaviour to linear and isotropic work hardening kinematic nonlinear. Note [R5.03.16].

3 Modeling A

3.1 Characteristics of modeling

Modeling AXIS

3.2 Characteristics of the grid

Many nodes: 4

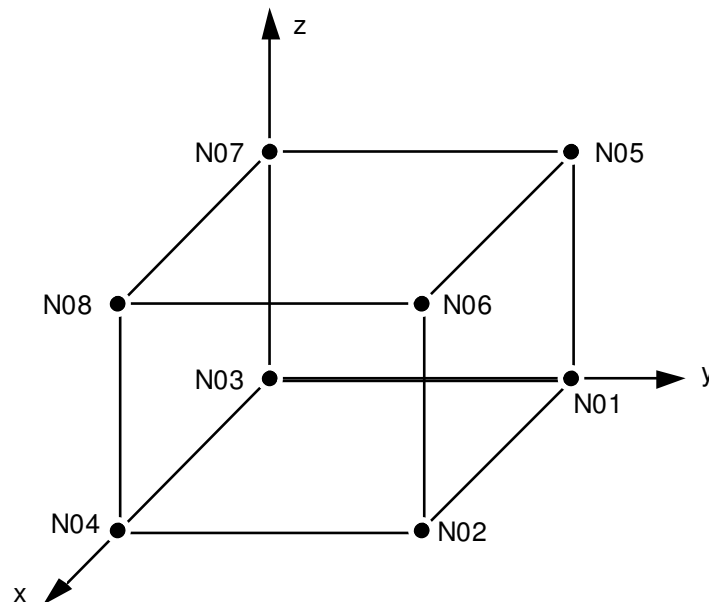
Many meshes and types: 1 QUAD4

3.3 Sizes tested and results

| Identification | Moments | Reference | Aster | % difference |
|----------------|---------|-----------|-------|--------------|
| σ_{yy} | 1 | 400 | 400 | 0 |
| σ_{yy} | 2 | 500 | 500 | 0 |
| σ_{yy} | 3 | - 380 | - 380 | 0 |
| σ_{yy} | 4 | - 464 | - 464 | 0 |

4 Modeling B

4.1 Characteristics of modeling



4.2 Characteristics of the grid

Many nodes: 8

Many meshes and types: 1 HEXA8 + 4 QUAD4 (faces)

4.3 Sizes tested and results

| Identification | Moments | Reference | Aster | % difference |
|----------------|---------|-----------|-------|--------------|
| σ_{yy} | 1 | 400 | 400 | 0 |
| σ_{yy} | 2 | 500 | 500 | 0 |
| σ_{yy} | 3 | - 380 | - 380 | 0 |
| σ_{yy} | 4 | - 464 | - 464 | 0 |

5 Modeling C

5.1 Characteristics of modeling

Modeling C_PLAN

5.2 Characteristics of the grid

Many nodes: 4
Many meshes and types: 1 QUAD4

5.3 Sizes tested and results

| Identification | Moments | Reference | Aster | % difference |
|----------------|---------|-----------|-------|--------------|
| σ_{yy} | 1 | 400 | 400 | 0 |
| σ_{yy} | 2 | 500 | 500 | 0 |
| σ_{yy} | 3 | - 380 | - 380 | 0 |
| σ_{yy} | 4 | - 464 | - 464 | 0 |

6 Summary of the results

Results provided by *Code_Aster* coincide with the values of reference, because the test is uniaxial, and the stress and strain state is homogeneous.