

## SDNL137 – Calculation of non-linear modes of a tube curved with two non-linearities of type annular contact

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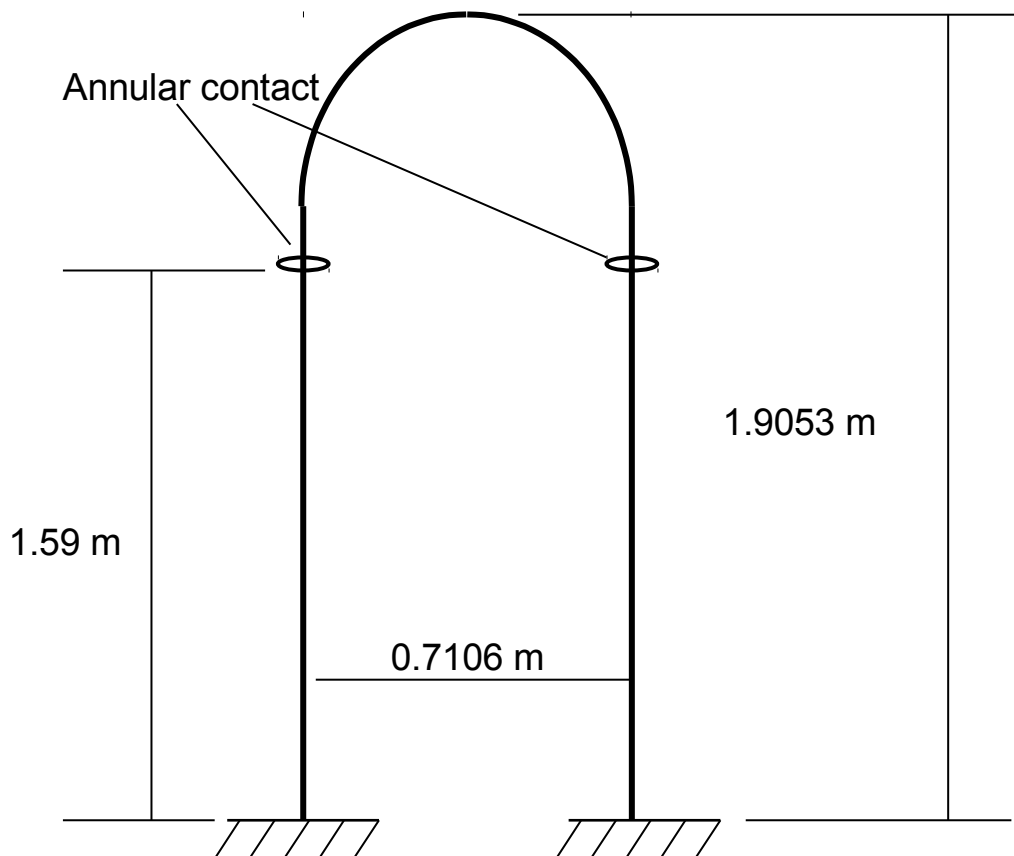
### Summary:

The objective of this test is to validate the calculation of non-linear mode with the operator `MODE_NON_LINE`. One particularly validates the system with a non-linearity of type annular contact.

## 1 Problem of reference

### 1.1 Geometry

The following structure is considered:



The tube has an external ray  $R_{ext} = 11.1110^{-3} m$  and a thickness of  $ep = 1.2710^{-3} m$

### 1.2 Properties of material

The material is elastic isotropic whose properties are:

- $E = 2.05610^{11} Pa$
- $\nu = 0.3$
- $\rho = 8357 kg/m^3$
- Rigidity of shock:  $K_{choc} = 410^6 N/m$

### 1.3 Boundary conditions and loadings

The game on the level of the annular contact is  $e = 2.910^{-4} m$ .

The annular contacts were isolated of 0.1e nodes of contact.

## 2 Reference solution

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One is interested in calculation of periodic solutions of the system characterizing the non-linear mode thus.

### 2.1 Method of calculating

For the resolution of the system, one uses method EHMAN [1]. One tries to follow the branch of the periodic solutions starting from the first mode of the subjacent linear system.

### 2.2 Sizes and results of reference

The selected reference variables are the couple frequency – energy and the stability of the periodic solution obtained.

A periodic solution is found for the couple frequency – energy such as:

$$5.2 \text{ Hz} < f < 5.5 \text{ Hz} \quad \text{and} \quad 7 \cdot 10^{-5} \text{ J} < E < 8 \cdot 10^{-5} \text{ J}$$

### 2.3 Uncertainties on the solution

Solution of not-regression.

### 2.4 Bibliographical references

- 1 E.H. MOUSSI, Analyzes vibrating structures equipped with located non-linearities with game using the non-linear modes. Doctorate 2013.

## 3 Modeling A

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### 3.1 Characteristics of modeling

A modeling is used POU\_D\_E.

### 3.2 Characteristics of the grid

The grid contains 10 elements of the type SEG2.

### 3.3 Sizes tested and results

One tests the couple frequency – energy by interpolation starting from the table produced by MODE\_NON\_LINE. A solution of not-regression is suggested. The values obtained are presented in the table below.

Frequency ( Hz )	Energy ( J )	Stability of the periodic solution
5.25698	$7.83624 \cdot 10^{-5}$	NON_EVALUE

## 4 Summary of the results

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This case test validates the operator of calculation of non-linear modes (`MODE_NON_LINE`) on a system having a non-linearity of type annular contact.

A solution of not-regression is suggested.