

SSLS133 - Flexbeam with variable thickness

Summary:

This test represents a quasi-static calculation of a flexbeam with variable thickness. It is embedded at an end, and is subjected to a vertical force at the other end. This test makes it possible to test the elements of voluminal hull SHB8 and SHB20 to manage the variations thicknesses. Four modelings are tested:

Finite elements SHB8 for a linear variation thickness of the plate (modeling A).

Finite elements SHB20 for a linear variation thickness of the plate (modeling B).

Finite elements SHB8 for a quadratic variation thickness of the plate (modeling C).

Finite elements SHB20 for a quadratic variation thickness of the plate (modeling D).

Displacements obtained are compared with the elastic analytical solution of a beam in inflection. This test makes it possible to show the capacities and the limits of the elements SHB8 and SHB20 to manage the variations thicknesses.

1 Problem of reference

1.1 Geometry

1.1.1 Plate with thickness varying linearly

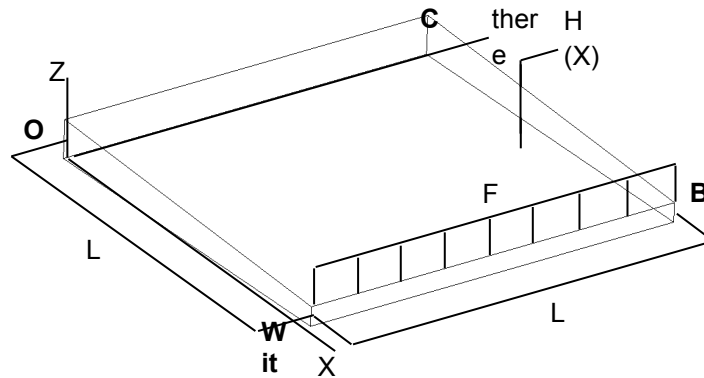


Figure 1.1.1-1 :

Length $L=100\text{ m}$, width $l=100\text{ m}$.

The thickness h vary linearly:

$$h(x) = ax + b$$

We pose $h(x=0)=h_1=10\text{ m}$ and $h(x=L)=h_2=5\text{ m}$ what gives us:

$$a = (h_2 - h_1)/L \text{ and } b = h_1$$

1.1.2 Plate with thickness varying quadratically

The thickness h vary in a quadratic way:

$$h(x) = ax^2 + bx + c$$

We pose $h(x=0)=h_1=10\text{ m}$, $h(x=L)=h_2=5\text{ m}$ and $h(x=L/2)=h_{12}=6,25\text{ m}$ what gives us

$$a = (2(h_1 + h_2) - 4h_{12})/L^2 , b = (4h_{12} - h_2 - 3h_1)/L \text{ and } c = h_1$$

1.2 Material properties

Young modulus: $E = 2.10^{11}\text{ Pa}$
Poisson's ratio: $\nu = 0.0$

1.3 Boundary conditions and loadings

Boundary conditions:

Embedded on the side OC : $u=v=w=0$, $\theta_x=\theta_y=\theta_z=0$

Loading:

At the end AB , one load uniformly distributed of resultant:

Force parallel with the axis Z ; $F_z=1N$

2 Reference solution

2.1 Method of calculating used for the reference solution

The results of reference are got by the theory of the elastic beams.

In the case of a linear variation thickness, vertical displacement at the end AB is given by [1]:

$$w(x) = -\frac{FL^2}{2EI_{y_1}c^3} \frac{\left(2Lcx + c^2x^2 - c^3x^2 + 2L(L+cx) \ln\left(\frac{L}{L+cx}\right)\right)}{(L+cx)}$$

With

$$c = \left(\frac{I_{y_2}}{I_{y_1}}\right)^{\frac{1}{3}} - 1 \quad \text{and} \quad I_{y_i} = \frac{bh_i^3}{12}$$

In the case of a quadratic variation thickness, it is possible to find a formula exact of displacement. However its general expression is sufficiently complex not to be able to be written here. We formulated the approximate function of vertical displacement according to x of our case:

$$w(x) = 3 \cdot 10^{-8} \frac{2x-200}{x^2-200x+20000} + 6 \cdot 10^{-10} \arctan(0.01x-1) - 3 \cdot 10^{-12}x + 7.71238 \cdot 10^{-10} m$$

2.2 Sizes and results of reference

Displacement of the points A and B according to Z .

2.3 Bibliographical references

[1] [V3.01.400] SSSL400 – non-prismatic Beam, subjected to efforts specific or distributed.

3 Modeling A

3.1 Characteristics of modeling

Element SHB8 and thickness varying linearly

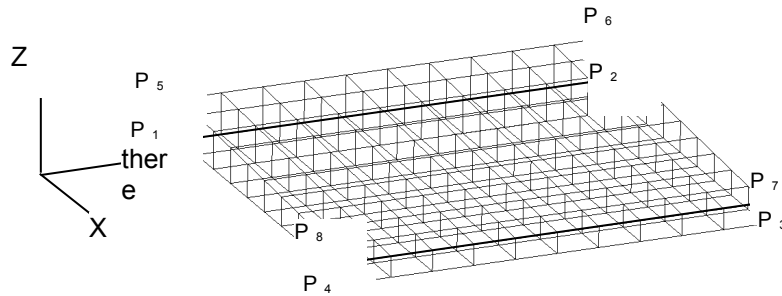


Figure 3.1-1 : Grid of modeling A

Cutting: a regular grid is considered in this modeling.

Regular grid:

100 meshes SHB8 : 10 according to the width, 10 according to the length, 1 according to the thickness

Boundary conditions:

All nodes inside the side $P_1P_2P_6P_5$: following blocked displacement X

All nodes on the edge P_1P_5 : following blocked displacement Y

All nodes on the edge P_2P_1 : following blocked displacement Z

Loading:

Force linearly distributed on the edge P_8P_7 : $F = 1$

Name of the nodes:

Not P_1	N022	Not P_5	N020
Not P_2	N002	Not P_6	N001
Not P_3	N102	Not P_7	N100
Not P_4	N172	Not P_8	N171

3.2 Characteristics of the grid

Many nodes: 242

Many meshes and types: 100 SHB8

3.3 Sizes tested and results

Regular grid:

Not	Size in unit	Reference	Aster	% difference
P_7	displacement W (m)	$3.2710 \cdot 10^{-10}$	$3.2711 \cdot 10^{-10}$	+0,004

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P₈ déplacement W (m) 3.2710 10⁻¹⁰ 3.2711 10⁻¹⁰ +0,004

4 Modeling B

4.1 Characteristics of modeling

Element SHB20 and thickness varying linearly

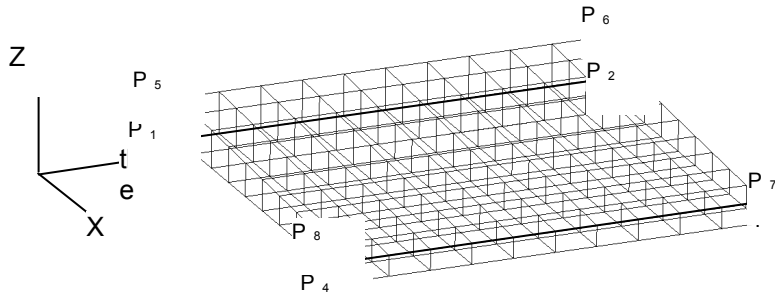


Figure 4.1-1 : Grid of modeling B

Cutting: a regular grid is considered in this modeling.

Regular grid:

100 meshes SHB20 : 10 according to the width, 10 according to the length, 1 according to the thickness

Boundary conditions:

All nodes inside the side $P_1 P_2 P_6 P_5$: following blocked displacement X

All nodes on the edge $P_1 P_5$: following blocked displacement Y

All nodes on the edge $P_2 P_1$: following blocked displacement Z

Loading:

Force linearly distributed on the edge $P_8 P_7$: $F = 1$

Name of the nodes:

Not P ₁	N347	Not P ₅	N340
Not P ₂	N579	Not P ₆	N572
Not P ₃	N006	Not P ₇	N002
Not P ₄	N074	Not P ₈	N067

4.2 Characteristics of the grid

Many nodes: 803

Many meshes and types: 100 SHB20

4.3 Sizes tested and results

Regular grid:

Not	Size in unit	Reference	Aster	% difference
P ₇	displacement W (m)	3.2710 10 ⁻¹⁰	3.2866 10 ⁻¹⁰	+0,476

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P₈ displacement W (m) 3.2710 10⁻¹⁰ 3.2866 10⁻¹⁰ +0,476

5 Modeling C

5.1 Characteristics of modeling

Element SHB8 and thickness varying quadratically

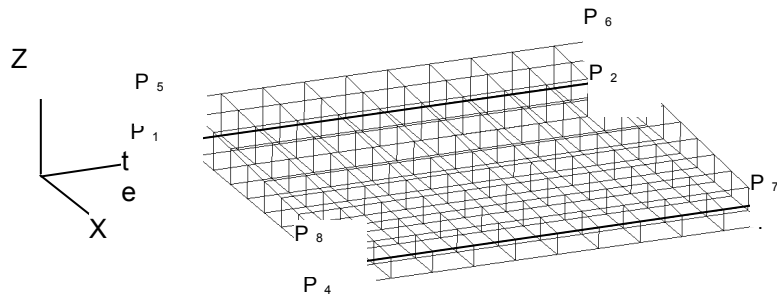


Figure 5.1-1 : Grid of modeling C

The characteristics are the same ones as for modeling A

Name of the nodes:

Not P ₁	N005	Not P ₅	N003
Not P ₂	N006	Not P ₆	N004
Not P ₃	N008	Not P ₇	N002
Not P ₄	N007	Not P ₈	N001

5.2 Characteristics of the grid

The grid is the same one as modeling A except for the thickness which varies here in a quadratic way.

5.3 Sizes tested and results

Regular grid:

Not	Size in unit	Reference	Aster	% difference
P ₇	displacement W (m)	4.7124 10 ⁻¹⁰	5.1212 10 ⁻¹⁰	+8.67
P ₈	displacement W (m)	4.7124 10 ⁻¹⁰	5.1212 10 ⁻¹⁰	+8.67

6 Modeling D

6.1 Characteristics of modeling

Element SHB20 and thickness varying quadratically

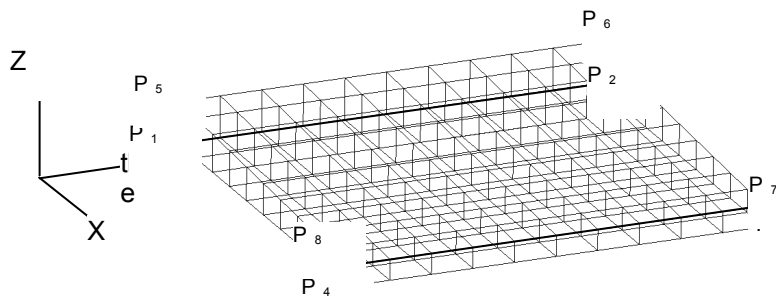


Figure 6.1-1 : Grid of modeling D

The characteristics are the same ones as for modeling *B*

Name of the nodes:

Not P ₁	N005	Not P ₅	N003
Not P ₂	N006	Not P ₆	N004
Not P ₃	N008	Not P ₇	N002
Not P ₄	N007	Not P ₈	N001

6.2 Characteristics of the grid

The grid is the same one as modeling *B* except for the thickness which varies here in a quadratic way.

6.3 Sizes tested and results

Regular grid:

Not	Size in unit	Reference	Aster	% difference
P ₇	displacement W (m)	4.7124 10 ⁻¹⁰	4.6754 10 ⁻¹⁰	-0,784
P ₈	displacement W (m)	4.7124 10 ⁻¹⁰	4.6754 10 ⁻¹⁰	-0,784

7 Summary of the results

In the case of a variation liniaire thickness of the plate, good solutions are obtained some is the finite element used (SHB8 or SHB20).

When the geometrical variation is of a quadratic nature, elements SHB20 provide more precise results (error $< 1\%$) that elements SHB8 (error $< 9\%$).