

## Operator CALC\_CHAMP

---

### 1 Goal

---

To create or supplement one `result` by calculating fields by element or with the nodes (forced, deformations,...).

The concept produced result either is created, or modified, i.e. the call to `CALC_CHAMP` is done in the following way:

```
resu = CALC_CHAMP ( RESULT = resu..., reuse = resu,...)
```

or

```
resul = CALC_CHAMP ( RESULT = resu,...)
```

## Contents

1 Goal.....	1
2 Syntax.....	3
2.1 Operands RESULTAT/MODELE/CHAM_MATER/CARA_ELEM/EXCIT.....	8
2.1.1 Operands RESULT.....	8
2.1.2 Operands MODEL/CHAM_MATER/CARA_ELEM.....	8
2.1.3 Keyword EXCIT.....	8
2.2 Selection of the meshes concerned with calculation.....	8
2.3 Selection of the sequence numbers.....	9
2.4 Localization of the fields.....	9
2.5 Dependence of the fields.....	10
2.6 Operands for the mechanical options.....	10
2.6.1 Options of calculation of the constraints (Operand CONSTRAINT).....	10
2.6.2 Options of calculation of the deformations (Operand DEFORMATION).....	13
2.6.3 Options of extraction of the internal variables (Operand VARI_INTERNE).....	14
2.6.4 Options of calculation of energy (Operand ENERGY).....	16
2.6.5 Options of calculation of criteria (Operand CRITERIA).....	19
2.6.6 Option of calculation of hydraulic flows (Operand HYDRAULICS).....	23
2.7 Operands for the thermal options.....	23
2.7.1 Operand THERMICS.....	23
2.8 Operands for the acoustic options.....	24
2.8.1 Operand ACOUSTICS.....	24
2.9 Operand for the nodal forces and reactions.....	25
2.9.1 Operand FORCE.....	25
2.9.2 Example 1: structure charged with nodal force (2 elements QUAD4).....	29
2.9.3 Example 2: structure with loading of temperature.....	30
2.9.4 Example 3: structure under loading distributed (beam).....	31
2.9.5 Example 4: calculation of the reactions of support at the bottom of a stopping.....	32
2.10 Calculation of a field user.....	34
2.10.1 Operand NOM_CHAM.....	34
2.10.2 Operand CRITERION.....	34
2.10.3 Operand FORMULA.....	34
2.10.4 Operand NORMALIZES.....	34
2.10.5 Operand NUME_CHAM_RESU.....	35
2.10.6 Example of calculation of a field user.....	35
2.11 Operand TITLE.....	35

## 2 Syntax

```

resu  [*] = CALC_CHAMP

(
  ◇ reuse = resu,
  ◇ MODEL = Mo, [model]
  ◇ CHAM_MATER = chmater, [cham_mater]
  ◇ CARA_ELEM = carac, [cara_elem]
  ◇ EXCIT = _F (
    ◆ LOAD = l_charge, [l_char_meca]
    ◇ / COEF_MULT = cm, [R]
      / FONC_MULT = Fm, [function]
    ◇ TYPE_CHARGE = 'FIXES',
  )
  ◇ # Selection of the meshes concerned with calculation
  / ALL = 'YES', [DEFECT]
  / | GROUP_MA = l_grma, [l_gr_maille]
    | MESH = l_mail, [l_maille]

  ◇ # Selection of the sequence numbers
  / TOUT_ORDRE = 'YES',
  / NUME_ORDRE = l_nuor, [l_I]
  / LIST_ORDRE = l_nuor, [listis]
  / NUME_MODE = l_numo, [l_I]
  / NOEUD_CMP = l_nomo, [l_K16]
  / NOM_CAS = nocas, [K16]
  / INST = l_inst, [l_R]
  / FREQ = l_freq, [l_R]
  / LIST_INST = l_inst, [listr8]
  / LIST_FREQ = l_freq, [listr8]

  ◇ | CRITERION = / 'RELATIVE', [DEFECT]
    / 'ABSOLUTE',
  | PRECISION = / prec,
    / 1.0E-6, [DEFECT]

# options for linear mechanical results

  ◆ RESULT = resu,

# options of calculation of the constraints (elements of continuous medium 2D
and 3D)

  ◇ CONSTRAINT = | 'EFGE_ELGA'
    | 'EFGE_ELNO'
    | 'EFGE_NOEU'
    | 'SIEF_ELGA'
    | 'SIEF_ELNO'
    | 'SIEF_NOEU'
    | 'SIGM_ELGA'
    | 'SIGM_ELNO'
    | 'SIGM_NOEU'
    | 'SIPM_ELNO'
    | 'SIPO_ELNO'
    | 'SIPO_NOEU'
    | 'SIRO_ELEM'

```

## # options of calculation of the deformations

```
◇ DEFORMATION =      |  \DEGE_ELGA'  
                    |  \DEGE_ELNO'  
                    |  \DEGE_NOEU'  
                    |  \EPME_ELGA'  
                    |  \EPME_ELNO'  
                    |  \EPME_NOEU'  
                    |  \EPSG_ELGA'  
                    |  \EPSG_ELNO'  
                    |  \EPSG_NOEU'  
                    |  \EPSI_ELGA'  
                    |  \EPSI_ELNO'  
                    |  \EPSI_NOEU'  
                    |  \EPVC_ELGA'  
                    |  \EPVC_ELNO'  
                    |  \EPVC_NOEU'
```

## # options of calculation of energies

```
◇ ENERGY =         |  \DISS_ELEM'  
                    |  \DISS_ELGA'  
                    |  \DISS_ELNO'  
                    |  \DISS_NOEU'  
                    |  \ECIN_ELEM'  
                    |  \ENEL_ELEM'  
                    |  \ENEL_ELGA'  
                    |  \ENEL_ELNO'  
                    |  \ENEL_NOEU'  
                    |  \EPOT_ELEM'  
                    |  \ETOT_ELEM'  
                    |  \ETOT_ELGA'  
                    |  \ETOT_ELNO'  
                    |  \ETOT_NOEU'
```

## # options of calculation of criteria

```
◇ CRITERIA =        |  \EPEQ_ELGA'  
                    |  \EPEQ_ELNO'  
                    |  \EPEQ_NOEU'  
                    |  \EPMQ_ELGA'  
                    |  \EPMQ_ELNO'  
                    |  \EPMQ_NOEU'  
                    |  \SIEQ_ELGA'  
                    |  \SIEQ_ELNO'  
                    |  \SIEQ_NOEU'
```

## # options of interpolation and extraction of internal variables

```
◇ VARI_INTERNE =    |  \VARC_ELGA'
```

# options for the nonlinear results (produced  
by STAT\_NON\_LINE or DYNA\_NON\_LINE) :

◆ RESULT = resu, / [evol\_noli]

# options of calculation of the constraints (elements of continuous medium 2D  
and 3D)

◇ CONSTRAINT = | `EFGE\_ELGA`  
| `EFGE\_ELNO`  
| `EFGE\_NOEU`  
| `SIEF\_ELNO`  
| `SIEF\_NOEU`  
| `SIGM\_ELGA`  
| `SIGM\_ELNO`  
| `SIGM\_NOEU`  
| `SIPO\_ELNO`  
| `SIPO\_NOEU`  
| `SIRO\_ELEM`

# options of calculation of the deformations

◇ DEFORMATION = | `DEGE\_ELGA`  
| `DEGE\_ELNO`  
| `DEGE\_NOEU`  
| `EPFD\_ELGA`  
| `EPFD\_ELNO`  
| `EPFD\_NOEU`  
| `EPFP\_ELGA`  
| `EPFP\_ELNO`  
| `EPFP\_NOEU`  
| `EPME\_ELGA`  
| `EPME\_ELNO`  
| `EPME\_NOEU`  
| `EPMG\_ELGA`  
| `EPMG\_ELNO`  
| `EPMG\_NOEU`  
| `EPSG\_ELGA`  
| `EPSG\_ELNO`  
| `EPSG\_NOEU`  
| `EPSI\_ELGA`  
| `EPSI\_ELNO`  
| `EPSI\_NOEU`  
| `EPSP\_ELGA`  
| `EPSP\_ELNO`  
| `EPSP\_NOEU`  
| `EPVC\_ELGA`  
| `EPVC\_ELNO`  
| `EPVC\_NOEU`

# options of calculation of energies

◇ ENERGY = | `DISS\_ELEM`  
| `DISS\_ELGA`  
| `DISS\_ELNO`  
| `DISS\_NOEU`  
| `ENEL\_ELEM`  
| `ENEL\_ELGA`

```

| 'ENEL_ELNO'
| 'ENEL_NOEU'
| 'ETOT_ELEM'
| 'ETOT_ELGA'
| 'ETOT_ELNO'
| 'ETOT_NOEU'

# options of calculation of criteria

◇ CRITERIA = | 'DERA_ELGA'
| 'DERA_ELNO'
| 'DERA_NOEU'
| 'ENDO_ELGA'
| 'ENDO_ELNO'
| 'ENDO_NOEU'
| 'EPEQ_ELGA'
| 'EPEQ_ELNO'
| 'EPEQ_NOEU'
| 'EPMQ_ELGA'
| 'EPMQ_ELNO'
| 'EPMQ_NOEU'
| 'INDL_ELGA'
| 'PDIL_ELGA'
| 'SIEQ_ELGA'
| 'SIEQ_ELNO'
| 'SIEQ_NOEU'

# options of interpolation and extraction of internal variables

◇ VARI_INTERNE = | 'VAEX_ELGA'
| 'VAEX_ELNO'
| 'VAEX_NOEU'
| 'VARC_ELGA'
| 'VARI_ELNO'
| 'VARI_NOEU'
| 'VAEX_ELNO'
| 'VAEX_NOEU'
| 'NOM_VARI = (cf. [#2.4.3.])
| 'NOM_VARI = (cf. [#2.4.3.])
| 'NOM_VARI = (cf. [#2.4.3.])

# options of calculation of hydraulic flows (elements THM)

◇ HYDRAULICS = | 'FLHN_ELGA'

# thermal options

◆ RESULT = resu, / [evol_ther]

◇ THERMIQUE= | 'FLUX_ELGA'
| 'FLUX_ELNO'
| 'FLUX_NOEU'
| 'HYDR_NOEU'
| 'SOUR_ELGA'
| 'ETHE_ELEM'

# acoustic options

◆ RESULT = resu, / [acou_harmo]
```

/ [mode\_acou]

```
◇ ACOUSTICS =          | 'PRAC_ELNO'  
                  | 'PRAC_NOEU'  
                  | 'PRME_ELNO'  
                  | 'INTE_ELNO'  
                  | 'INTE_NOEU'
```

## # options for the generalized forces and nodal reactions

```
◆ RESULT = resu,
```

```
◇ FORCE =              | 'FORC_NODA'  
                  | 'REAC_NODA'
```

## # calculation of a field user

```
◇ CHAM_UTIL = _F (  
    ◆ NOM_CHAM = ncham,  
    ◆ / CRITERION = | 'VMIS',  
                  | 'INVA_2'  
                  | 'TRACE',  
    / FORMULA = l_form, [formula]  
    / NORMALIZES = | 'L2',  
                  | 'FROBENIUS'  
    ◆ NUME_CHAM_RESU = digital, [I]  
    ),  
◇ TITLE = title, [l_Kn]  
◇ INFORMATION = / 1, [DEFECT]  
                / 2,  
)
```

## 2.1 Operands RESULTAT/MODELE/CHAM\_MATER/CARA\_ELEM/EXCIT

### 2.1.1 Operands RESULT

◆ RESULT = `resu`

Name of the structure of data result to enrich. This argument can be same as that used for the concept enriched by the operator, or a different name, which will create a new structure of data result.

**Note:**

*In the majority of the situations, the structure of data `resu` contains all the necessary information with the calculation of the options: the model, the field of material, characteristics elementary, loadings. Keywords `MODEL`, `CHAM_MATER`, `CARA_ELEM` and `EXCIT` are thus useless.*

### 2.1.2 Operands MODEL/CHAM\_MATER/CARA\_ELEM.

◇ MODEL = `Mo`

Name of the model on which the efforts are calculated, constraints, deformations, etc. It is optional because it can be extracted the result.

◇ CHAM\_MATER = `chmater`

Material field associated with the model `Mo`. This keyword is optional and must be provided only in exceptional cases (voluntary modification of material for example).

◇ CARA\_ELEM = `carac`

Elementary characteristics associated with the model `Mo` if it contains elements of structure or if the isoparametric elements are affected by a local reference mark of anisotropy. This keyword is optional because it can be extracted the result.

### 2.1.3 Keyword EXCIT

This keyword factor (optional) makes it possible to specify the thermal or mechanical loadings to use for the calculation of the options, instead of those which were useful in the structural analysis of data specified under the keyword `RESULT`.

The definition of this keyword is identical to that of the orders which built the structure of data `resu`: to see the orders `MECA_STATIQUE` [U4.51.01], `STAT_NON_LINE` [U4.51.03], `DYNA_LINE_HARM` [U4.53.11], and `DYNA_LINE_TRAN` [U4.53.02].

## 2.2 Selection of the meshes concerned with calculation

Keywords `ALL`, `GROUP_MA` and `MESH` allow the user to choose the meshes on which it wishes to do his elementary calculations of postprocessing.

```
/ ALL = 'YES'
```

All the meshes (carrying finite elements) will be treated. It is the value by default.

```
/ | GROUP_MA = l_grma  
| MESH = l_maille
```

Only meshes included in `l_grma` and/or `l_maille` will be treated.

## 2.3 Selection of the sequence numbers

Use of the keywords TOUT\_ORDRE, NUM\_ORDRE, INST, FREQ is described in the document [U4.71.00].

## 2.4 Localization of the fields

In the continuation of the document one will not explicitly specify the localization of the fields. Indeed, the localization is given in the name of the field (and thus of the option):

- Field by element: \*\_ELEM
- Field at the points of Gauss per element: \*\_ELGA
- Field with the nodes by element: \*\_ELNO
- Field with the nodes: \*\_NOEU

The fields, for the majority, are calculated natively at the points of Gauss (\*\_ELGA).

Fields with the nodes by element (\*\_ELNO) are obtained by extrapolation starting from the field at the points of Gauss (detailed method in [R3.06.03]).

Fields with the nodes (\*\_NOEU) are obtained starting from the fields with the nodes by element by making a simple arithmetic mean (not balanced by the size of the meshes) of the values recorded on the elements in a given node.

### Notice 1:

*For the calculation of the equivalents, the fields with the nodes by element (\*\_ELNO) are not obtained by extrapolation starting from the field at the points of Gauss. Extrapolation is made on the stress field or of deformation then one calculates the field of equivalent.*

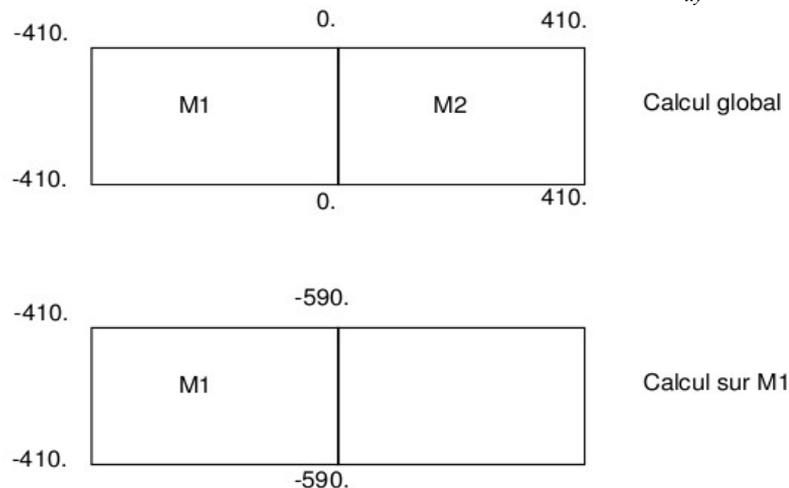
### Notice 2:

*The averages with the nodes of computed fields in local reference marks are licit only if the angles between these reference marks are weak. In the contrary case, they do not have a direction.*

### Notice 3:

*When the keyword GROUP\_MA or MESH are well informed for the calculation of an option \*\_NOEU, the arithmetic mean is made on the selected meshes. Thus this result is different from that obtained by doing a total calculation then restricted with the only selected meshes.*

*Example: One considers a structure of which the shear stress  $\sigma_{xy}$  is worth:*



*In total calculation,  $\sigma_{xy}$  is worthless on  $M1 \cap M2$  like average of two opposite values. These values are far from being worthless, as calculation shows it on M1 only. The values on the border of the required field are thus to interpret with precaution.*

For the elements of structures which have under-points (multifibre plates, hulls, beams, pipes), fields of the type \*\_ELGA and \*\_ELNO are calculated on all the under-points. To obtain one field on only one under-point (a layer and a level for example), an extraction should be made *via* the operator POST\_CHAMP (options EXTR\_COQUE, EXTR\_PMF and EXTR TUYAU). Moreover this intermediate operation is essential to calculate a field of the type \*\_NOEU for these elements of structure: fields of the type \*\_NOEU indeed never have under-point.

Finally the options of calculation of energy never produce fields under-point. Indeed for the elements of structure, the field is integrated in the thickness (integration made on the under-points).

## 2.5 Dependence of the fields

The calculation of a field can require the preliminary calculation of one or more other fields. Thus for example to calculate a field \*\_NOEU it is necessary to have the same field by element to the nodes \*\_ELNO and at the points of Gauss \*\_ELGA.

This dependence is solved by the operator CALC\_CHAMP who carries out the calculation of the intermediate fields automatically. It is thus not necessary for the user to know the tree of dependence of the options.

Only the fields explicitly required by the user are saved in the structure of data result.

## 2.6 Operands for the mechanical options

### 2.6.1 Options of calculation of the constraints (Operand CONSTRAINT)

The components of the generalized effort and stress fields are detailed in the document [U2.01.05].

```
| `EFGE_ELGA`  
| `EFGE_ELNO`  
| `EFGE_NOEU`
```

Calculation of the generalized efforts (elements of structure).

It acts as of an extraction of the efforts contained in the field SIEF\_ELGA/STRX\_ELGA (case of the elements of beams/pipes or discrete), that is to say of a calculation by integration of the constraints (case of the multifibre elements of beams or plates and hulls).

#### Notice 1:

*LE field EFGE\_ELNO is not always an extrapolation of the field EFGE\_ELGA ; in particular for a linear calculation where this field is calculated directly starting from displacement. This is why certain components are not calculated (put at zero) into non-linear.*

#### Notice 2:

*For the offset plates, the efforts are calculated in the "plan" of the grid. If one wishes these efforts in the average "plan" of the plate, the order should be used POST\_CHAMP / COQUE\_EXCENT.*

```
| `SIEF_ELGA`  
| `SIEF_ELNO`  
| `SIEF_NOEU`
```

Calculation of the state of stress (forced or efforts generalized according to modeling) starting from displacements (linear elasticity), to see [U2.01.05].

#### Note:

*The field `SIEF\_ELGA` is calculated natively by the non-linear operators of resolution. It is always present in a structure of data result of the type evol\_noli.*

```
| `SIGM_ELGA`
```

| `SIGM\_ELNO`  
 | `SIGM\_NOEU`

Calculation of the state of stress.

It is actually about an extraction of the constraints contained in the field SIEF\_ELGA, to see [U2.01.05].

| `SIPO\_ELNO`  
 | `SIPO\_NOEU`

Calculation of the constraints in the section of beam broken up into contributions of each generalized effort.

List of the components of the field:

SN	Contribution of the normal effort $N$ with $\sigma_{xx}$ , $\sigma_{xx} = \frac{N}{A}$
SMFY	Contribution of the bending moment $MFY$ with $\sigma_{xx}$ , $\sigma_{xx} = z \frac{MFY}{I_Y}$
SMFZ	Contribution of the bending moment $MFZ$ with $\sigma_{xx}$ , $\sigma_{xx} = -y \frac{MFZ}{I_Z}$
SVY	Contribution of the shearing action $VY$ with $\sigma_{xy}$ , $\sigma_{xy} = \frac{VY a_Y}{A}$ $a_Y$ coefficient of shearing in the direction $y$
SVZ	Contribution of the shearing action $VZ$ with $\sigma_{xz}$ , $\sigma_{xz} = \frac{VZ a_Z}{A}$ $a_Z$ coefficient of shearing in the direction $z$
SMT	Contribution of the torque $MX$ with $\sigma_{yz}$ , $\sigma_{yz} = \frac{MX R_T}{J_x}$

The constraints above are expressed in the local reference mark, i.e. the principal reference mark of inertia of the cross-section [R3.08.01].

Values of  $\sigma_{xx}$  had at the two bending moments are the maximum values of those calculated in  $Y_{min}$ ,  $Y_{max}$  on the one hand, and in  $Z_{min}$ ,  $Z_{max}$  in addition (except for a general section where it is the user who provides the localization of the extremum with the keyword  $RY$ ,  $RZ$  and  $RT$  cf. AFFE\_CARA\_ELEM [U4.42.01]).

For a rectangular section:

- one calculates the value of SMFY in  $z = HZ/2$ ,
- one calculates the value of SMFZ in  $y = HY/2$ .

For a circular section, one calculates the values of SMFY and SMFZ for  $y$  and  $z$  being worth  $R$ .

| `SIPM\_ELNO`

Calculation of the constraints maximum and minimum in the section of beam starting from the generalized efforts (linear elasticity).

The same remark as for SIPO\_ELNO applies a general section in the case of.

| `SIRO\_ELEM`

Calculation of the constraints projected on the skin of a volume (for example on the facings of a hydraulic work).

List of the components of the field:

SIG_NX SIG_NY SIG_NZ	Components $\sigma_X, \sigma_Y, \sigma_Z$ in the total reference mark of $\vec{\sigma}_n$
SIG_N	Value $SIG_N$
SIG_TX SIG_TY SIG_TZ	Components $\sigma_X, \sigma_Y, \sigma_Z$ in the total reference mark of $\vec{\sigma}_t$
SIG_T1X SIG_T1Y SIG_T1Z	Components $\sigma_X, \sigma_Y, \sigma_Z$ in the total reference mark of $\vec{\sigma}_{t1}$
SIG_T1	Eigenvalue $SIG_{T1}$
SIG_T2X SIG_T2Y SIG_T2Z	Components $\sigma_X, \sigma_Y, \sigma_Z$ in the total reference mark of $\vec{\sigma}_{t2}$
SIG_T2	Eigenvalue $SIG_{T2}$

These fields are evaluated starting from a stress field calculated on the voluminal meshes (MODELISATION= `3D` or `3D\_SI`):

- Identification of the voluminal meshes corresponding to the facets of the group of surface meshes. For each facet (surface mesh), one chooses the voluminal mesh located on the side "-" normal at the facet. If there is no voluminal mesh of with dimensions "-" facet, one does not calculate SIRO\_ELEM on this facet;
- Recovery of the constraints 3D to assign them to the nodes faces;
- Average of each component of the tensor of the constraints in the center of the faces of elements;
- One places oneself in a reference mark composed by the normal vector  $\vec{n}$  with the facet and the plan of the facet. A noted tensor is obtained  $[\sigma]$ .
- One evaluates  $[\sigma]\vec{n} = \vec{\sigma}_n + \vec{\sigma}_t$ ,  $\vec{\sigma}_n$  being a vector colinéaire with  $\vec{n}$ .  $\vec{\sigma}_t$  is then a vector representing the shearing which is negligible in the case of the faces upstream/downstream of a stopping. One notes  $\vec{\sigma}_n = SIG_N \vec{n}$  and  $SIG_N$  indicate the presence of traction if it is positive and of compression if it is negative.
- One thus places oneself on the assumption of a negligible shearing

$$[\sigma] = \begin{bmatrix} \sigma_{2D} & 0 \\ 0 & SIG_N \end{bmatrix}$$

One seeks the vectors of principal constraints corresponding to  $\sigma_{2D}$ : the vectors are thus obtained  $\vec{\sigma}_{t1}$  and  $\vec{\sigma}_{t2}$  who are in the plan of the facet and the eigenvalues  $SIG_{T1}$  and  $SIG_{T2}$

**Notice 1:**

*In the case of facets plunged in volume, the user has the possibility thanks to the order MODI\_MALLAGE/ORIE\_PEAU\_3D/GROUP\_MA\_VOLU to reorientate this normal as it wishes it. It can thus choose the voluminal mesh which will be used for calculation. So side "-", one finds a mesh of "joint" (which is voluminal), the calculation of SIRO\_ELEM is impossible because the constraints stored in the elements of joint do not allow calculation detailed above.*

**Notice 2:**

*If one informs TOUT= ' OUI ', the list of the meshes is filtered to keep only the meshes of skin.*

## 2.6.2 Options of calculation of the deformations (Operand DEFORMATION)

The components of the fields of deformation are detailed in the document [U2.01.05].

| `DEGE\_ELGA`

Calculation of the deformations generalized starting from displacements. This option has direction only for the elements of structure of plate and pipe, not for the beams  
The generalized deformations are obtained in the local reference mark of the element.

| `DEGE\_ELNO`

| `DEGE\_NOEU`

Calculation of the deformations generalized starting from displacements. This option has direction only for the elements of structure of beam, plate and pipe.  
The generalized deformations are obtained in the local reference mark of the element.

| `EPFD\_ELGA`

| `EPFD\_ELNO`

| `EPFD\_NOEU`

Calculation of the deformations of creep of desiccation, for the models BETON\_UMLV\_FP and BETON\_BURGER\_FP.

| `EPFP\_ELGA`

| `EPFP\_ELNO`

| `EPFP\_NOEU`

Calculation of the deformations of clean creep associated with the model GRANGER\_FP, with the model BETON\_UMLV\_FP or with the model BETON\_BURGER\_FP.

| `EPME\_ELGA`

| `EPME\_ELNO`

| `EPME\_NOEU`

Calculation of the “mechanical” deformations starting from displacements. This calculation is done in theory of “ **small displacements** ”. The calculated deformations are equal to the total deflections minus the thermal deformations. The deformations of drying and hydration are also withdrawn as well as the deformations of pressure of fluid and the deformations unelastic. On the other hand the deformations of creep are not withdrawn.

$$\varepsilon_{ij}^m(u) = \frac{1}{2}(u_{i,j} + u_{j,i}) - \varepsilon^{th}$$

| `EPMG\_ELGA`

| `EPMG\_ELNO`

| `EPMG\_NOEU`

Calculation of the “mechanical” deformations starting from displacements. This calculation is done in theory of “ **large displacements** ”. The calculated deformations are equal to the total deflections minus the thermal deformations.

$$E_{ij}^m(u) = \frac{1}{2}(u_{i,j} + u_{j,i} + u_{k,i}u_{k,j}) - \varepsilon^{th}$$

| `EPSG\_ELGA`

| `EPSG\_ELNO`

| `EPSG\_NOEU`

Calculation of the deformations of Green-Lagrange.

$$E_{ij}(u) = \frac{1}{2}(u_{i,j} + u_{j,i} + u_{k,i}u_{k,j})$$

| `EPSI\_ELGA`

```
| `EPSI_ELNO`
| `EPSI_NOEU`
```

Calculation of the deformations starting from displacements.

$$\varepsilon_{ij}(u) = \frac{1}{2}(u_{i,j} + u_{j,i})$$

For the elements of structure, these deformations are obtained in the local reference mark of the element.

```
| `EPSP_ELGA`
| `EPSP_ELNO`
| `EPSP_NOEU`
```

Calculation of the unelastic deformations starting from the field of displacement  $u$ , constraints  $\sigma$ , temperature  $T$ , possible unelastic deformations  $\varepsilon^a$ , and of the internal variables,

$$\varepsilon^p = \varepsilon(u) - A^{-1} \sigma - \varepsilon^{th}(T) - \varepsilon^a - \varepsilon^{fl}$$

where  $\varepsilon^{fl}$  is the clean deformation of creep of Granger.

```
| `EPVC_ELGA`
| `EPVC_ELNO`
| `EPVC_NOEU`
```

Calculation of the deformations related to the variables of order. For the moment only the following components are defined:

- thermal deformations: EP THER\_L, EP THER\_T, EP THER\_N such as:  $\varepsilon_i^{th} = \alpha_i (T - T_{ref})$ ;  $i \in \{L, T, N\}$  (if the material is isotropic, the 3 components are equal),  $T$  being the temperature and  $\alpha_i$  the thermal dilation coefficient;
- withdrawal of drying EPSECH (used for the laws describing the behavior of the concrete)  $\varepsilon^{sech} = -K_{dessic} (S_{ref} - S)$ ,  $S$  being the variable of order drying and  $K_{dessic}$  the coefficient of withdrawal of desiccation;
- withdrawal of hydration EPHYDR (used for the laws describing the behavior of the concrete)  $\varepsilon^{hydr} = -B_{endog} h$ ,  $h$  being the variable of order hydration, and  $B_{endog}$  being the endogenous coefficient of withdrawal.
- Deformation related to the pressure of fluid (for thermo-hydro-mechanics with a resolution by chaining): EPPTOT such as:  $\varepsilon^{ptot} = \frac{b}{3K} p_{tot}$ ,  $p_{tot}$  is the variable of order total pressure of fluid,  $b$  is the coefficient of Biot,  $K$  is the modulus of elasticity.

### 2.6.3 Options of extraction of the internal variables (Operand VARI\_INTERNE)

```
| `VAEX_ELGA`
| `VAEX_ELNO`
| `VAEX_NOEU`
```

Extraction of internal variables in THM only.

The goal of this option is to be able post-to treat the internal variables in THM in a more convivial way. The principle of these fields is to extract from the field VARI\_ELGA (or VARI\_ELNO) (one and only one) the variable intern who interests us via a keyword without having to know his name in the field VARI\_\*.

List of the possible components of the field (the field has only one component, that chosen by the user via NOM\_VARI):

DPORO	Variation of the porosity of material
DRHOLQ	Variation of the density of material
DPVP	Variation of the steam pressure
SATLIQ	Saturation of the liquid
EVP	Cumulated voluminal plastic deformation
IND ETA	Mechanical indicator of state
D	Value of the damage
IND END	Indicator of damage
TEMP MAX	Maximum temperature
GAMP	Plastic deformation déviatoire cumulated
PCR	Critical pressure
SEUIL HYD	Hydrous threshold
IND HYD	Hydrous indicator of irreversibility
PCOHE	Pressure of cohesion
COMP ROC	Behavior of the rock
SEUIL ISO	Isotropic threshold
ANG DEV	Angle of the threshold déviatoire
X11	Components of the kinematic tensor of work hardening
X22	Components of the kinematic tensor of work hardening
X33	Components of the kinematic tensor of work hardening
X12	Components of the kinematic tensor of work hardening
X13	Components of the kinematic tensor of work hardening
X23	Components of the kinematic tensor of work hardening
DIST DEV	Distance standardized with the threshold déviatoire
DEV_SUR_CRIT	Relationship between the threshold déviatoire and the critical threshold deviatoric
DIST ISO	Distance standardized with the isotropic threshold
NB ITER	Iteration count internal
STOP	Value of the local test of stop of the iterative process
NB REDE	Number of local recutting of the step of time
SIGN	Sign of the contracted product of the deviatoric constraint by the deviatoric plastic deformation

◇ NOM\_VARI = / nom\_vari, [TXM]

Name of the internal variable.

**Notice 1:**

When the variable to be extracted is not part of the internal variables of the laws concerned, an alarm is emitted but the field is affected all the same with *R8VIDE* (*()*) (number very large reality about *1.0E+308*).

**Notice 2:**

The field *VAEX\_NOEU* is calculated from *VAEX\_ELNO* and not by extraction of the field *VARI\_NOEU*.

| 'VARC\_ELGA'

Calculation of the variables of orders having been used for a mechanical calculation.

List of the components of the field:

TEMP	Cf documentation of the order AFFE_MATERIAU [U4.43.03] for the definition of each component.
HYDR	
SECH	
CORR	
IRRA	
PTOT	
DIVU	
NEUT1	
NEUT2	

**Note:**

All the components are systematically calculated. The variables which were not defined are initialized with the value `R8VIDE ()` (Nombre real very large about  $1.0E+308$ ).

- | 'VARI\_ELNO'
- | 'VARI\_NOEU'

Calculation of the internal variables.

List of the components of the field:

V1	Variable interns 1
...	
VI	Variable interns I
...	
Vn	Internal variable N

The number and the type of these internal variables are specific to each model of behavior (cf. [U4.51.11]).

**Note:**

The field 'VARI\_ELGA' is calculated natively by the non-linear operators of resolution. It is always present in a SD result of the type `evol_noli`.

## 2.6.4 Options of calculation of energy (Operand ENERGY)

- | 'DISS\_ELEM'

Calculation of the energy dissipated by the damage. The field obtained has only one component of name 'ENDO'.

List of the components of the field:

ENDO	Energy dissipated by the damage
------	---------------------------------

**Note:**

Valid only for the elements `DKTG` and the law `GLRC_DM`. Its expression is given in [R7.01.32].

- | 'DISS\_ELGA'
- | 'DISS\_ELNO'
- | 'DISS\_NOEU'

Calculation of the density of energy dissipated by the damage. The field obtained has only one component of name 'ENDO'.

List of the components of the field:

ENDO	Energy dissipated by the damage
------	---------------------------------

**Note:**

Valid only for the elements *DKTG* and the law *GLRC\_DM*. Its expression is given in [R7.01.32].

'ECIN\_ELEM'

Calculation of the kinetic energy.

$$E_c = \frac{1}{2} m v^2$$

List of the components of the field:

TOTAL	Kinetic energy
Additional components for the plates and hulls:	
MEMBRANE INFLECTIO N	Contributions to the kinetic energy (cf [R3.07.03])
Additional components for the curved beams:	
PLAN_XY PLAN_XZ	Contributions to the kinetic energy (cf [R3.08.01])
Additional components for the discrete ones:	
DX DY DZ DRX DRY MARTINI DRZ	Contributions to the kinetic energy

'ENEL\_ELEM'

Calculation of elastic energy.

$$E_p = \frac{1}{2} \sigma A^{-1} \sigma$$

List of the components of the field:

TOTAL	Elastic energy
Additional components for the plates and hulls: Contributions to elastic energy (cf [R3.07.03])	
MEMBRANE INFLECTIO N SHEAR COUPL_MF	Elastic energy out of membrane Elastic energy in inflection Elastic energy in shearing Elastic energy of coupling membrane-inflection

**Note:**

Into non-linear (*STAT\_NON\_LINE*, *DYNA\_NON\_LINE*,...) components *SHEAR* and *COUPL\_MF* are worthless.

'ENEL\_ELGA'

'ENEL\_ELNO'

'ENEL\_NOEU'

Calculation of the density of energy elastic.

List of the components of the field:

TOTAL	Elastic energy
Additional components for the plates and hulls: Contributions to elastic energy (cf [R3.07.03])	
MEMBRANE	Elastic energy out of membrane
INFLECTIO	Elastic energy in inflection
N	Elastic energy in shearing
SHEAR	Elastic energy of coupling membrane-inflection
COUPL_MF	

**Note:**

Into non-linear (STAT\_NON\_LINE, DYNA\_NON\_LINE,...) components SHEAR and COUPL\_MF are worthless.

| `EPOT\_ELEM`

Calculation of the potential energy of deformation, starting from the field of displacement  $u$  and of the fields of temperature  $T$  :

List of the components of the field:

TOTAL	Potential energy
Additional components for the plates and hulls:	
MEMBRANE	Contributions to the potential energy (cf [R3.07.03])
INFLECTIO	
N	
Additional components for the right beams:	
TRAC_COM	Contributions to the potential energy (cf [R3.08.01])
TORSION	
FLEX_Y	
FLEX_Z	
Additional components for the curved beams:	
PLAN_XY	Contributions to the potential energy (cf [R3.08.01])
PLAN_XZ	
Additional components for the discrete ones:	
DX	Contributions to the potential energy
DY	
DZ	
DRX	
DRY	
MARTINI	
DRZ	

- for the elements of continuous mediums 2D and 3D:

$$E_{pot} = \frac{1}{2} \int_{element} \boldsymbol{\varepsilon}(U) \cdot \mathbf{A} \cdot \boldsymbol{\varepsilon}(U) dv - \int_{element} \boldsymbol{\varepsilon}(U) \cdot \mathbf{A} \cdot \boldsymbol{\varepsilon}^{th}(U) dv + \frac{1}{2} \int_{element} \boldsymbol{\varepsilon}^{th}(U) \cdot \mathbf{A} \cdot \boldsymbol{\varepsilon}^{th}(U) dv$$

- for the elements of beams:

$$E_{pot} = \frac{1}{2} u^T \cdot \mathbf{K}_e \cdot u - u^T \cdot \mathbf{B}^T \cdot \mathbf{A} \cdot \boldsymbol{\varepsilon}^{th} + \frac{1}{2} \boldsymbol{\varepsilon}^{th} \cdot \mathbf{A} \cdot \boldsymbol{\varepsilon}^{th}$$

- for the elements of plates and hulls:

$$E_{pot} = \frac{1}{2} u^T \cdot \mathbf{K}_e \cdot u - u^T \cdot \mathbf{B}^T \cdot \mathbf{A} \cdot \boldsymbol{\varepsilon}^{th}$$

| `ETOT\_ELEM`

Calculation of the increment of total deformation energy enters the moment running and the previous moment.

List of the components of the field:

TOTAL	Increment of total deformation energy
-------	---------------------------------------

- | 'ETOT\_ELGA'
- | 'ETOT\_ELNO'
- | 'ETOT\_NOEU'

Calculation of the increment of density of total deformation energy enters the moment running and the previous moment.

List of the components of the field:

TOTAL	Increment of total deformation energy
-------	---------------------------------------

## 2.6.5 Options of calculation of criteria (Operand CRITERIA)

- | 'DERA\_ELGA'
- | 'DERA\_ELNO'
- | 'DERA\_NOEU'

Calculation of the local indicator of discharge and indicator of loss of radially [R4.20.01].

List of the components of the field:

DCHA_V	Indicator of discharge calculated on the deviative tensor of the constraints
DCHA_T	Indicator of discharge calculated on the total tensor of the constraints
IND_DCHA	Indicator allowing to know if the discharge would remain elastic or if there would be a risk of plasticization if a pure kinematic work hardening were used
VAL_DCHA	In the case of indicate the proportion of exit of the criterion abusive discharge
X11 X22 X33 X12 X13 X23	Components of the kinematic tensor used for the calculation of IND_DCHA
RADI_V	Indicator of the variation of the direction of the constraints between the moments $t$ and $t + \Delta t$
ERR_RADI	Error $\eta$ had with the discretization in time, directly connected to the rotation of the normal on the surface of load

DCHA\_V and DCHA\_T express, in the two cases, the relative variation of the standard of the constraints within the meaning of Von Misès:  $I_1 = \frac{\|\sigma(M, t + \Delta t)\| - \|\sigma(M, t)\|}{\|\sigma(M, t + \Delta t)\|}$ , the standard being function of the behavior (isotropic work hardening or linear kinematics)

IND\_DCHA can take the following values:

- 0 : unconstrained initial value;
- 1 : if elastic load;
- 2 : if plastic load;
- -1 : if licit elastic discharge (whatever the type of work hardening);
- -2 : if abusive discharge (one would have plasticized with a kinematic work hardening).

RADI\_V is given by the following relation:

$$I_2 = 1 - \frac{|\boldsymbol{\sigma}(M, t) \cdot \Delta \boldsymbol{\sigma}|}{\|\boldsymbol{\sigma}(M, t)\| \|\Delta \boldsymbol{\sigma}\|}$$

This quantity is worthless when the radiality is preserved during the increment of time.

ERR\_RADII is the angle enters  $\mathbf{n}^-$ , the normal with the criterion of plasticity at the beginning of the step of time (urgent  $t^-$ ), and  $\mathbf{n}^+$ , the normal with the criterion of plasticity calculated at the end of the step of time (urgent  $t^+$ ) in the following way:

$$\eta = \frac{1}{2} \|\Delta \mathbf{n}\| = \frac{1}{2} \|\mathbf{n}^+ - \mathbf{n}^-\| = \left| \sin\left(\frac{\alpha}{2}\right) \right|$$

That provides a measurement of the error (also used to refine the step of time [U4.51.11]. This criterion is operational for the elastoplastic behaviors of Von Mises with work hardening isotropic, kinematic linear and mixed: VMIS\_ISOT\_LINE, VMIS\_ISOT\_TRAC, VMIS\_ISOT\_PUIS, VMIS\_CINE\_LINE, VMIS\_ECMI\_LINE, VMIS\_ECMI\_TRAC, and for the behaviors élasto-visco-plastics of Chaboche: VMIS\_CIN1\_CHAB, VMIS\_CIN2\_CHAB, VMIS\_CIN2\_MEMO, VISC\_CIN1\_CHAB, VISC\_CIN2\_CHAB, VISC\_CIN2\_MEMO.

**Note:**

The calculation of these options requires to compare the stress fields with the moments  $t_i$  and  $t_{i+1}$ . The result is arranged with the sequence number associated with the moment  $t_i$ .

The indicator of discharge is calculated by:  $ID = \frac{\|\boldsymbol{\sigma}_{i+1}\| - \|\boldsymbol{\sigma}_i\|}{\|\boldsymbol{\sigma}_{i+1}\|}$ .

By default, calculation is done for the sequence numbers 1 with  $n-1$ . But if one specifies the list of moment (with "holes" possibly), calculation will relate to only the required moments but it will always compare the moment  $t_i$  with the moment  $t_{i+1}$  in the list of the moments having been used to do the non-linear calculation.

- | 'ENDO\_ELGA'
- | 'ENDO\_ELNO'
- | 'ENDO\_NOEU'

Calculation of the damage  $d$  starting from the tensor of the constraints and cumulated plastic deformation  $p$ .

List of the components of the field:

TRIAX	Rate of triaxiality
SI_ENDO	Equivalent constraint of damage of Lemaître-Sermage
COENDO	Constraint of damage of Lemaître-Sermage standardized
DOM_LEM	Damage of Lemaître-Sermage

The rate of triaxiality  $\alpha$  is given by the following relation:

$$\alpha = \frac{\sigma_h}{\sigma_{eq}}$$

and the equivalent constraint of damage  $\sigma^*$  :

$$\sigma^* = \sigma_{eq} \sqrt{\frac{2}{3}(1+\nu) + 3(1-2\nu)\alpha^2}$$

$$\mathbf{s} = \boldsymbol{\sigma} - \frac{1}{3} \text{tr}(\boldsymbol{\sigma}) \cdot \mathbf{Id}$$

with:  $\sigma_{eq} = \sqrt{\frac{3}{2} \mathbf{s} : \mathbf{s}}$

$$\sigma_h = \frac{1}{3} \text{tr}(\boldsymbol{\sigma})$$

The kinetics of damage is given by the law of Lemaître-Sermage:

$$\dot{d} = \left[ \frac{Y}{S} \right]^s \dot{p} \text{ if } p \geq p_{seuil} \text{ with } Y = \frac{\sigma^{*2}}{2E(1-D)^2}$$

where  $S$  and  $s$  are coefficients characteristic of material and  $p_{seuil}$  the threshold of damage related to the energy stored in material (if  $s=1$  one obtains the classical law of Lemaître).

| 'EPEQ\_ELGA'  
 | 'EPEQ\_ELNO'  
 | 'EPEQ\_NOEU'  
 | 'EPMQ\_ELGA'  
 | 'EPMQ\_ELNO'  
 | 'EPMQ\_NOEU'

Calculation of the calculated deformations equivalent starting from the fields EPSE\_\*, or EPME\_\*).

List of the components of the field:

INVA_2	Equivalent deformation of Von Mises
PRIN_1 PRIN_2 PRIN_3	Principal deformations, lines in the ascending order
INVA_2SG	Equivalent deformation of Von Mises signed by the trace of $\boldsymbol{\varepsilon}$
VECT_1_X VECT_1_Y VECT_1_Z VECT_2_X VECT_2_Y VECT_2_Z VECT_3_X VECT_3_Y VECT_3_Z	Principal directions

The equivalent deformation of Von Mises is given by the following expression:

$$\text{INVA}_2 = \sqrt{\frac{2}{3} \text{dev}(\boldsymbol{\varepsilon})_{ij} \text{dev}(\boldsymbol{\varepsilon})_{ji}} \text{ with } \text{dev}(\boldsymbol{\varepsilon})_{ij} = \varepsilon_{ij} - \frac{1}{3} \text{tr}(\boldsymbol{\varepsilon}) \delta_{ij}$$

**Note:**

*It is noted that the equivalent deformations obtained from EPSE\_\* and EPME\_\* are identical. Indeed, the difference between the two tensors is a spherical tensor (thermal deformation). Like equivalent deformation is obtained starting from the second invariant of the diverter, the spherical tensor "disappears" when the diverter is taken.*

| 'INDL\_ELGA'

Calculation of the indicator of localization, based on the acoustic tensor (criterion of RICE).

List of the components of the field:

	Indicator of localization
INDEX	0 if $\det(N.H.N) > 0$ 1 if not, which corresponds has the initiation of the localization
DIR1	First normal at the zone of localization
DIR2	Second normal at the zone of localization
DIR3	Third normal at the zone of localization
DIR4	Fourth normal at the zone of localization

This indicator defines a state from which the local problem of integration of the behavior loses its character of unicity. It is defined by:  $\det(N.H.N) \leq 0$ , where  $H$  appoint the tangent operator and  $N$  the normal with the directions of localization.

**Note:**

The method is developed only in the case 2D and for the laws of behavior of the type DRUCK\_PRAGER and HUJEUX.

| `PDIL\_ELGA`

Calculation of the module of rigidity of microphone-dilation.

List of the components of the field:

A1\_LC2                    Module of rigidity of microphone-dilation

The option PDIL\_ELGA provides within the framework of the mediums of second gradient of dilation the value of the module A1\_LC2, allowing to control the periodicity of the noncommonplace solution of the initially homogeneous problem [R5.04.03].

The calculation of A1\_LC2 is obtained via the evaluation of a function depending on the geometrical orientation of the material band considered. The angular discretization currently imposed is equal to  $0.1^\circ$ .

**Note:**

The method is developed only for the laws of behavior of the type DRUCK\_PRAGER and HUJEUX.

| `SIEQ\_ELGA`

| `SIEQ\_ELNO`

| `SIEQ\_NOEU`

Calculate calculated constraints equivalent starting from the stress fields.

List of the components of the field:

VMIS	Equivalent constraint of Von Mises
TRESCA	Constraint of Tresca
PRIN_1 PRIN_2 PRIN_3	Principal constraints, lines in the ascending order
VMIS_SG	Equivalent constraint of Von Mises signed by the trace of $\sigma$
VECT_1_X VECT_1_Y VECT_1_Z VECT_2_X VECT_2_Y VECT_2_Z VECT_3_X VECT_3_Y VECT_3_Z	Principal directions
TRSIG	Trace of $\sigma$
TRIAX	Rate of triaxiality

The equivalent constraint of Von Mises is given by the following expression:

$$VMIS = \sqrt{\frac{3}{2} s_{ij} s_{ji}} \text{ with } s_{ij} = \sigma_{ij} - \frac{1}{3} tr(\sigma) \delta_{ij}$$

The rate of triaxiality is given by the following expression:

$$TRIAX = \frac{TRSIG}{VMIS}$$

## 2.6.6 Option of calculation of hydraulic flows (Operand HYDRAULICS)

| 'FLHN\_ELGA'

Calculation of hydraulic flows in THM  $\Phi_{ij} = M_{ij} \cdot \mathbf{v}$  on the elements of edge (2D or 3D) starting from the vector flow with the nodes.

$M_{ij}$  is the hydraulic vector flow of the component  $ij$ .

List of the components of the field:

FH11	
FH22	
FH12	
FH21	

## 2.7 Operands for the thermal options

### 2.7.1 Operand THERMICS

| 'FLUX\_ELGA'

| 'FLUX\_ELNO'

| 'FLOW\_NOEU'

Calculation of the heat flows starting from the temperature.

List of the components of the field:

FLOW FLUY FLUZ	Heat flow in the three directions of space (in the average layer for the hulls)
Additional components for the hulls:	
FLUX_INF FLUY_INF FLUZ_INF	Heat flow in the three directions of space in lower skin
FLUX_INF FLUY_INF FLUZ_INF	Heat flow in the three directions of space in higher skin

| 'HYDR\_NOEU'

Calculation of the hydration.

List of the components of the field:

HYDR	Hydration
------	-----------

**Note:**

The field 'HYDR\_ELNO' is calculated natively by the non-linear operator of thermics THER\_NON\_LINE for the modeling of the concrete [R7.01.12].

| 'PENNYR\_ELGA'

Calculation of a source of heat.

List of the components of the field:

SOUR	Source of heat
------	----------------

This source is calculated starting from an electric potential via the law of Ohm. This electric potential must be calculated by the operator THER\_LINEAIRE [U4.54.01] by making the analogies necessary. This source can be then used in a thermal calculation via the keyword SOUR\_CALCULEE order AFFE\_CHAR\_THER [U4.44.02].

| 'ETHE\_ELEM'

Calculation of thermal energy to balance starting from the field of temperature  $T$ .

List of the components of the field:

TOTAL	Thermal energy
-------	----------------

## 2.8 Operands for the acoustic options

### 2.8.1 Operand ACOUSTICS

| 'INTE\_ELNO'

| 'INTE\_NOEU'

Calculation of the acoustic intensity. The definitions are in [R4.02.01].

List of the components of the field:

INTX_R	Acoustic intensity, real part according to axis X
INTY_R	Acoustic intensity, real part according to the axis there
INTZ_R	Acoustic intensity, real part according to axis Z
INTX_I	Acoustic intensity, imaginary part according to axis X
INTY_I	Acoustic intensity, imaginary part according to the axis there
INTZ_I	Acoustic intensity, imaginary part according to axis Z

- | 'PRAC\_ELNO'
- | 'PRAC\_NOEU'

Calculation of the pressure to the nodes partly real, imaginary part and decibels.

List of the components of the field:

PRES_I	Acoustic pressure, real part
PRES_R	Acoustic pressure, imaginary part
DB	Acoustic pressure in decibel

- | 'PRME\_ELNO'

Calculation of the pressure to the nodes for the elements FLUID.

List of the components of the field:

DB	Acoustic pressure in decibel
----	------------------------------

## 2.9 Operand for the nodal forces and reactions

### 2.9.1 Operand FORCE

- | 'FORC\_NODA'

Calculation of the nodal forces generalized starting from the constraints at the points of Gauss.

List of the components of the field:

DX DY DZ	Nodal forces
Additional components for the elements of structure:	
DRX DRY MARTINI DRZ	Nodal forces (moments)

The nodal forces correspond to the direction finite elements with the interior forces taking part in the equilibrium equations. The calculation of the generalized nodal forces  $\mathbf{F}_K$  is done in the following way:

$$\sum_K \mathbf{F}_K \cdot \mathbf{v}_K = \int_{\Omega} \boldsymbol{\sigma} \cdot \boldsymbol{\varepsilon}(\mathbf{v}_K) d\Omega = \sum_K \int_K \boldsymbol{\sigma}^K \cdot \boldsymbol{\varepsilon}(\mathbf{v}_K) dK = \sum_K \int_K \boldsymbol{\sigma}^K \cdot \mathbf{B} \cdot \mathbf{v}_K dK$$

with  $\boldsymbol{\sigma}^K$  constraints at the points of Gauss of the element  $K$  ;

$\mathbf{B}$  the operator finite elements of generalized deformations (matrix connecting the deformations of the 1<sup>er</sup> order with generalized displacements);

$\mathbf{v}_K$  generalized unit elementary displacement.

From where: 
$$\mathbf{F}_K = \left\{ \int_K {}^t \mathbf{B} \cdot \boldsymbol{\sigma}^K dK \right\} .$$

The dimension of the nodal forces is dual of that of  $\mathbf{v}_K$  to give a work (in Joules).

For the elements of beam and the elements discrete, the constraints at the points of Gauss are in fact the nodal efforts generalized in the reference mark of the element (obtained by the product of the matrix of rigidity of the element by displacement and by taking account of the efforts of thermal origin and the efforts distributed). The calculation of the nodal forces is done by projecting the nodal efforts contained in the field of reference symbol 'SIEF\_ELGA'

in the total reference mark. The summation above on the elements applies then. Components DX, DY and DZ the forces give and DRX, DRY MARTINI and DRZ moments.

For the axisymmetric elements, integration in  $\theta$  is done on a sector of 1 radian. If one wants the integral of the surface effort on all the disc it is thus necessary to multiply by  $2\pi$ .

For the elements in plane deformation, is calculated on a tape of width unit. The calculated nodal forces are thus by way of forces per unit of length. If one wants to calculate the nodal forces being exerted on a structure of width  $l$ , it is necessary to multiply the result in D\_PLAN by  $l$ , with this close the assumption of plane deformation is not valid close to the two faces. There will be thus an approximate result.

For the solid elements (3D, 2D and bars), them FORC\_NODA in general have the dimension of a force. It is about a field on the nodes of the grid where the value in a node is obtained starting from the constraints calculated on the convergent elements with this node, thus their values thus vary when the grid changes. In the absence of loading distributed, balance imposes their nullity in an interior node, while they correspond to the reaction on the supports where a kinematic relation is imposed (case of an imposed displacement).

In the case of hulls, components DX, DY and DZ they give FORC\_NODA (of dimension of a force) in the total reference mark of the grid. These components are built with the normal efforts and cutting-edges in the hull. Components DRX, DRY MARTINI and DRZ they give FORC\_NODA (of one moment dimension) in the total reference mark of the grid, built with the bending moments in the hull.

In (thermo) hydro-mechanical, cf § 8, [R7.01.10], the generalized nodal forces associated with each component correspond to the mechanical forces and flows. If one notes  $\mathbf{Q}^T \sigma_0$  the result of FORC\_NODA, for the hydraulic equations, then for a step of time  $\Delta t$ , one a:

$$\int_{\Omega} \mathbf{Q}^T \sigma_0 \cdot p^* d\Omega = -\Delta t \int_{\Omega} \mathbf{M}^- \cdot \nabla p^* d\Omega$$

**Note:**

To note that flows are taken at the moment  $t^-$  because of  $\theta$  - diagram employed, cf [R7.01.10].

In FORC\_NODA :

- with the degree of freedom PRE1 in saturated for example is associated water flow  $-\Delta t \int_{\Omega} (\mathbf{M}_{vp} + \mathbf{M}_w)^- \cdot \nabla p^* d\Omega$
- with the degree of freedom PRE2 in unsaturated flow with the gas component is associated  $-\Delta t \int_{\Omega} (\mathbf{M}_{ad} + \mathbf{M}_{as})^- \cdot \nabla p^* d\Omega$
- with the degree of freedom TEMP the heat flux is associated  $-\Delta t \int_{\Omega} \mathbf{q}^- \cdot \nabla T^* d\Omega$

with  $\mathbf{q}$  heat flux and  $\mathbf{M}_w$ ,  $\mathbf{M}_{vp}$ ,  $\mathbf{M}_{as}$  and  $\mathbf{M}_{ad}$  hydraulic flows of liquid water, the vapor, the air (or all other composing) dry and of the air dissolved in the liquid. These data correspond respectively to the constraints generalized of Code\_Aster  $M_1^1, M_1^2, M_2^1, M_2^2$ , cf § 2.2, [R7.01.10].

| 'REAC\_NODA'

Calculation of the nodal forces of reactions generalized with the nodes, the constraints at the points of Gauss and of the loadings.

List of the components of the field:

DX DY DZ	Nodal reactions
Additional components for the elements of structure:	
DRX DRY MARTINI DRZ	Nodal reactions (moments)

The generalized nodal reactions correspond to the direction finite elements with the forces exerted on the supports (boundary conditions) taking part in the equilibrium equations.

In statics, for the concepts result of the type `evol_elas`, `mult_elas`, `fourier_elas` or `evol_noli`, the calculation of the generalized nodal reactions  $\mathbf{R}_K$  is done by:

$$\sum_K \mathbf{R}_K \cdot \mathbf{v}_K = \int_{\Omega} \boldsymbol{\sigma} \cdot \boldsymbol{\varepsilon}(\mathbf{v}_K) d\Omega - \mathbf{L}(\mathbf{v}_K)$$

with  $\mathbf{v}_K$  generalized unit elementary displacement,

$$\mathbf{L}(\mathbf{v}_K) = \int_{\Omega} \mathbf{f} \cdot \mathbf{v}_K d\Omega + \int_{\Gamma} \mathbf{F}_s \cdot \mathbf{v}_K d\Gamma + \sum_i \mathbf{F}_i \cdot \mathbf{v}_{Ki}$$

where  $\mathbf{f}$  are the voluminal forces,

$\mathbf{F}_s$  surface generalized forces,

$\mathbf{F}_i$  specific forces generalized with the node  $i$ .

The vector of the nodal reactions generalized on the element  $K$  is thus obtained starting from the generalized nodal forces:

$$\mathbf{R}_K = \mathbf{F}_K - \int_K \mathbf{f} dK - \int_{\partial K} \mathbf{F} \partial K - \sum_i \mathbf{F}_{iK}$$

in other words, one cuts off with the nodal forces the generalized external forces applied to the element  $K$ .

**Note:**

*To note that the loading of temperature does not appear in the external forces: it intervenes in the expression of the constraints via the law of behavior.*

In dynamics, to obtain the nodal reactions, it is advisable to in addition remove the efforts of inertia (acceleration) and damping related to speed.

**Note:**

*Currently in Code\_Aster the contributions of damping directly related to speed on the nodal reactions are neglected.*

For the concepts result of the type `mode_meca` (resulting from modal calculations) the formula is:

$$\sum_K \mathbf{R}_K \cdot \mathbf{v}_K = \int_{\Omega} \boldsymbol{\sigma}(\boldsymbol{\varepsilon}(\mathbf{u})) \cdot \boldsymbol{\varepsilon}(\mathbf{v}_K) d\Omega - \omega^2 (\mathbf{M} \cdot \mathbf{u}) \cdot \mathbf{v}_K$$

where  $\boldsymbol{\sigma}(\boldsymbol{\varepsilon}(\mathbf{u}))$  are the generalized modal constraints,

$\mathbf{M}$  is the matrix of mass,

$\omega$  the own pulsation,

$\mathbf{u}$  the field of displacement generalized of the mode,

$\mathbf{v}_K$  generalized unit elementary displacement.

For the concepts result of the type `dyna_trans` resulting from linear transitory dynamic calculations (`DYNA_LINE_TRAN`, or `DYNA_TRAN_MODAL` by the means of `REST_GENE_PHYS`), of type `dyna_harmo` resulting from harmonic calculations (`DYNA_LINE_HARM`) or of type `evol_noli` resulting from calculation dynamic non-linear transients (`DYNA_NON_LINE`) the expression of the generalized nodal reactions is obtained by:

$$\sum_K \mathbf{R}_K \cdot \mathbf{v}_K = \int_{\Omega} \boldsymbol{\sigma} \cdot \boldsymbol{\varepsilon}(\mathbf{v}_K) d\Omega + (\mathbf{M} \ddot{\mathbf{u}}) \cdot \mathbf{v}_K - \mathbf{L}(\mathbf{v}_K)$$

where  $\mathbf{M}$  is the matrix of mass;  
 $\ddot{\mathbf{u}}$  the field of generalized acceleration;  
 $\mathbf{L}$  the vector of the generalized external forces applied,  
 $\mathbf{v}_K$  generalized unit elementary displacement.

#### Notice 1:

*The nodal reactions are worthless in any interior point of the model and are not worthless a priori in a point of the edge subjected to a kinematic boundary condition (or with efforts of contact).  
However the fact of neglecting the contribution of damping in dynamics can create a light variation compared to the exact result.*

#### Notice 2:

*If the keyword `GROUP_MA` is informed, the options '`FORC_NODA`' and '`REAC_NODA`' are calculated as follows:*

*$\mathbf{F}_K$  is calculated only on the elements requested then assembled. The result is different from a total calculation on all the field then reduced to the required elements. The established method makes it possible to measure the reaction of a piece of model on another.*

*Caution: the calculation of '`REAC_NODA`' on a subset of the model (via the keyword `GROUP_MA`) must be made with prudence. Example 4 below illustrates this kind of calculation.*

#### Notice 3:

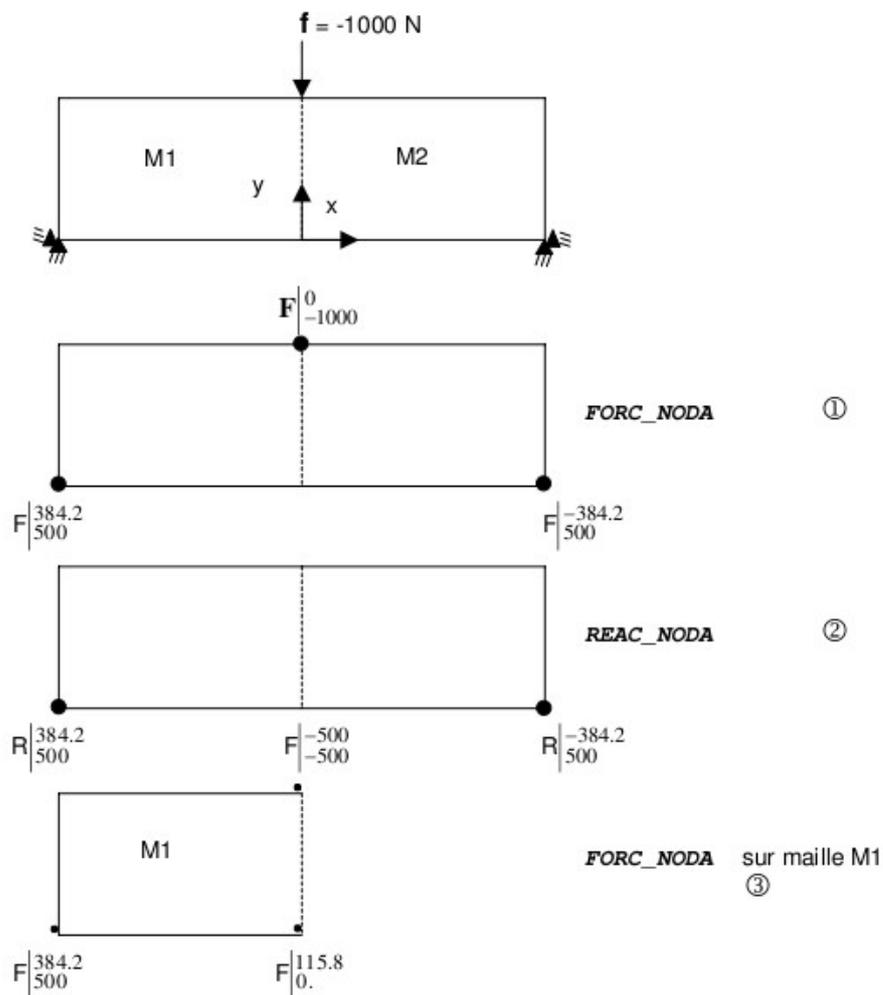
*Only the resultant of the forces or the nodal reactions on a group of nodes has a physical direction (this group must correspond to at least an element of the model, for example an edge subjected to a boundary condition). It can be calculated with `POST_RELEVE_T` [U4.81.21].*

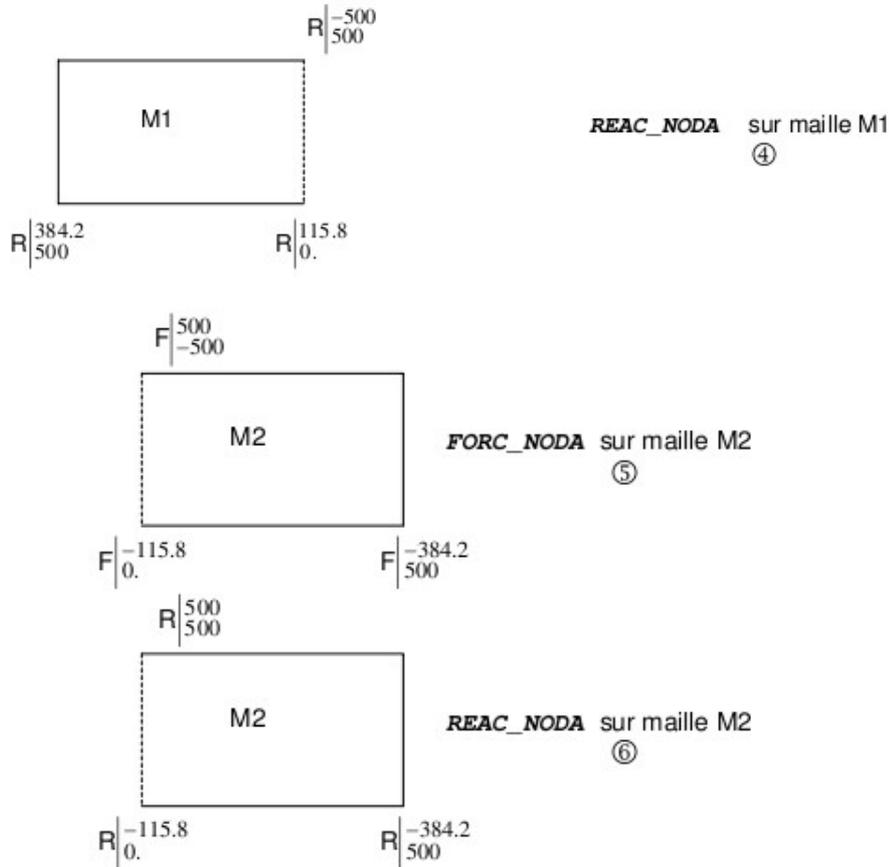
*Punctually, the field `FORC_NODA` or `REAC_NODA` does not have to be interpreted because the value in a node is directly related to the smoothness of the grid. Moreover the sign of these forces on the nodes of the same element can be against-intuitive whereas it is perfectly in agreement with the theory of the finite elements (for example on meshes `QUAD8` located at the interface of a pure compression zone, the signs of the nodal forces at the tops and the mediums are opposite).*

#### Notice 4:

*The calculation of `REAC_NODA` account of the loadings distributed on the beams takes. Since you vary this loading on a non-linear calculation (change of `EXCIT` of a step of time to the other), the calculation of `REAC_NODA` is prohibited. It is necessary to divide its postprocessing into "packages" of sequence numbers, for which the loading is constant (i.e. it uses the same concept `AFFE_CHAR_MECA` in `EXCIT`).*

## 2.9.2 Example 1: structure charged with nodal force (2 elements QUAD4)





On this example, reactions to the nodes (2) are quite equal to the nodal forces (1) less the loading. They represent the reactions to the supports of the structure.

If one restricts calculation with the mesh  $M1$ , forces (3) to the nodes belonging to the border enters  $M1$  and  $M2$  are different. They represent the reaction of the model formed by  $M1$  with the model formed by  $M2$ . To note that the nodal loading is divided by two because the two meshes contribute to it. Nodal reactions (4) are still equal to the nodal forces minus the loading.

On the calculation restricted with the mesh  $M2$ , nodal forces (5) according to  $Ox$  are of contrary sign to the calculation restricted with the mesh  $M1$ , illustrating the principle of the action and the reaction.

### 2.9.3 Example 2: structure with loading of temperature

Data:

$$E = 1.10^9 \text{ Pa}$$

$$\nu = 0.3$$

$$\alpha = 1.10^{-6}$$

Results:

$$F_y = -3.410^4 \text{ N}$$

$$F_{1x} = 7.8 \cdot 10^3 \text{ N}$$

$$F_{2x} = -1.2 \cdot 10^3 \text{ N}$$

On this example, the nodal forces and the nodal reactions coincide because the only loading is a loading temperature.

If one restricts calculation with the mesh  $M2$ , forces according to  $OY$  remain the same ones but are different according to  $OX$ .

### 2.9.4 Example 3: structure under loading distributed (beam)

One considers a structure of type beam fixed and subjected to a loading of gravity on his higher half.

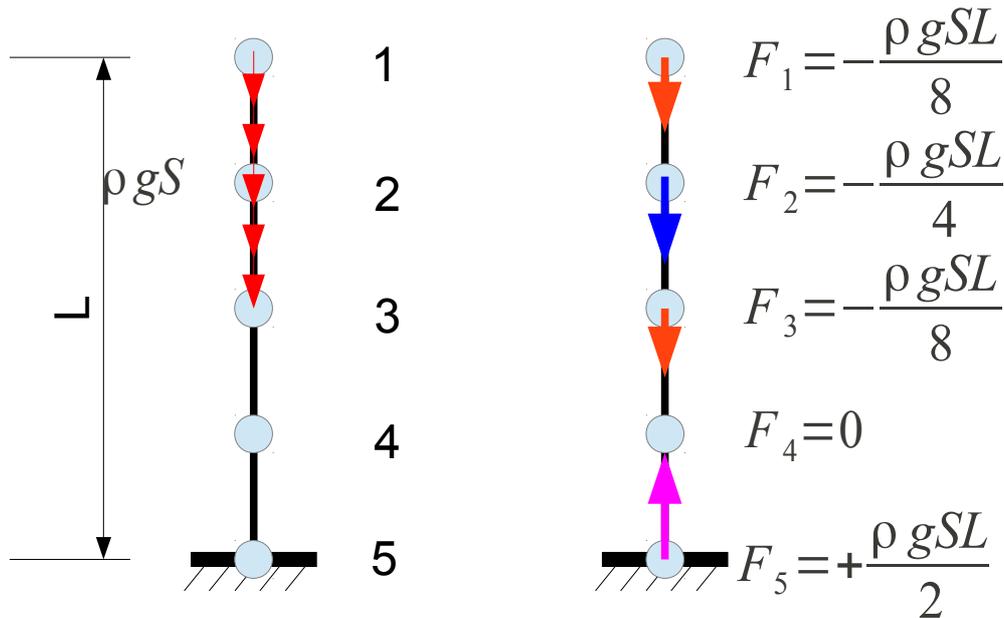


Figure 2.9.4-1: structure under loading distributed (left), FORC\_NODA (right-hand side)

On this kind of structure, if one restricts the calculation of the forces and the nodal reactions to a under-part of the elements, FORC\_NODA and REAC\_NODA will not give the same result on the interface between the part isolated and the rest from the structure as shown in the figure 2.9.4-2 (on the force  $F_3$ ).

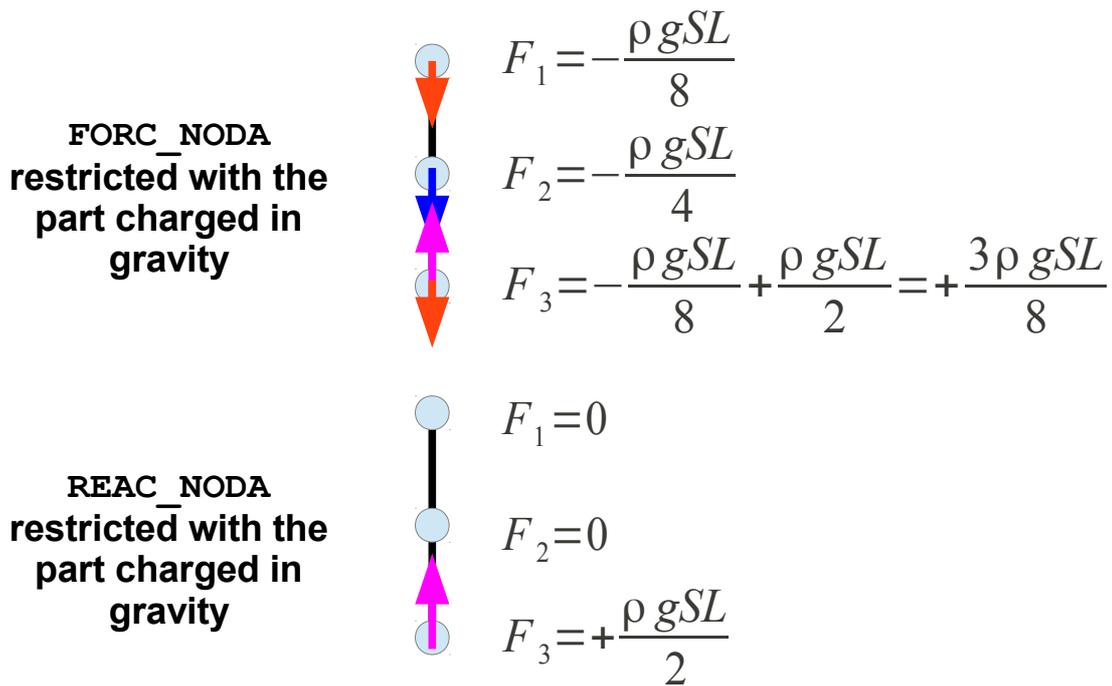


Figure 2.9.4-2: insulation of part of the structure

## 2.9.5 Example 4: calculation of the reactions of support at the bottom of a stopping

In this example, one schematizes (very coarsely!) a stopping in 2D. The stopping is represented by a triangle DEF posed on a foundation represented by a rectangle ABCG (see diagram below).

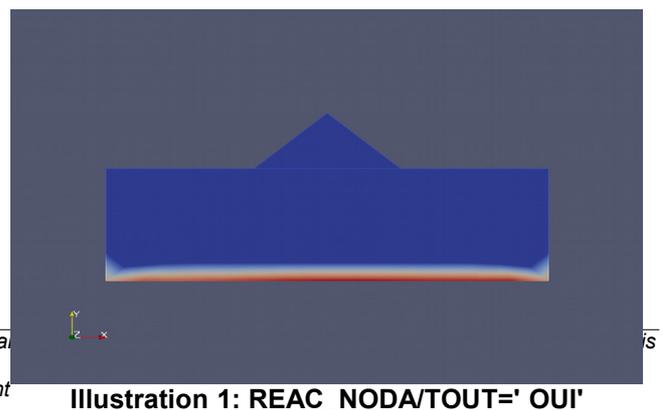
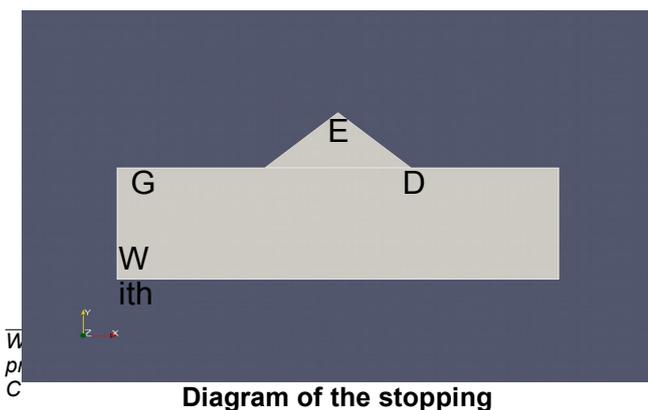
One would like to calculate the reactions of support of the stopping on his foundation.

The loadings are:

- Gravity (which applies to the stopping and its foundation)
- The loading of pressure of to the water reserve (side upstream) applied to the edges CD and OF.
- The foundation is embedded on AB.

On the following illustrations, one represented the standard of the field REAC\_NODA when the keyword is used GROUP\_MA various ways:

- Illustration 1: one does not use GROUP\_MA (TOUT=' OUI ')
- Illustration 2: GROUP\_MA=' BARRAGE '
- Illustration 3: GROUP\_MA= ( 'STOPPING' , 'OF' )
- Illustration 4: GROUP\_MA= ( 'STOPPING' , 'OF' , 'CD' )



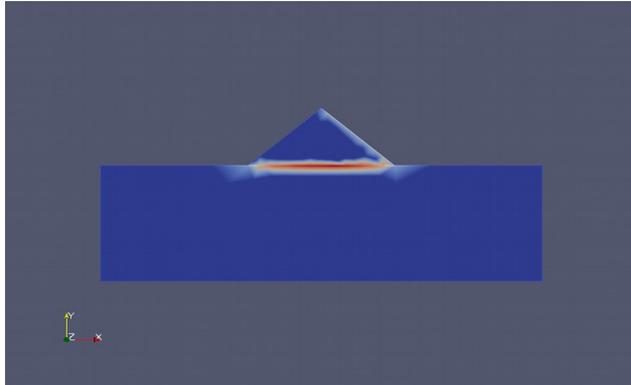


Illustration 2: REAC\_NODA/GROUP\_MA='  
BARRAGE'

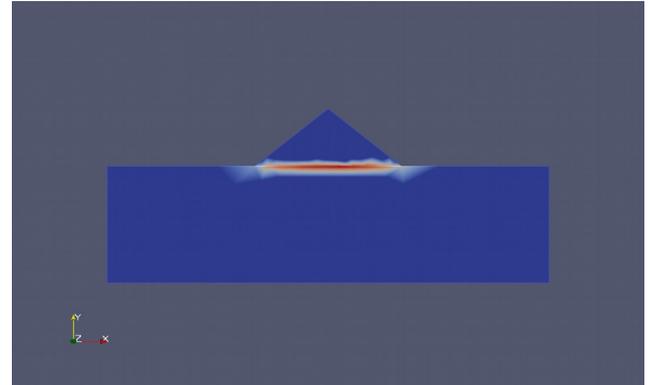


Illustration 3: REAC\_NODA/GROUP\_MA=  
( 'STOPPING', 'OF' )

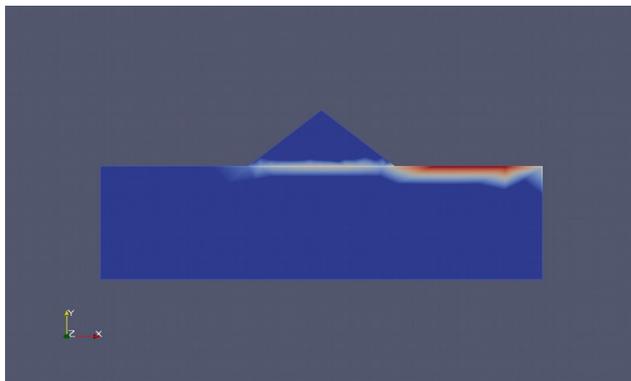


Illustration 4: REAC\_NODA/GROUP\_MA=  
( 'STOPPING', 'OF', 'CD' )

#### Comments:

- Illustration 1 shows that when the keyword is not used `GROUP_MA`, the reaction of support are not-worthless only on the edge of the model where one imposes displacements here ( `AB` ).
- Illustration 2 shows that if one calculates `REAC_NODA` on the only group `STOPPING` (formed only of "voluminal" elements) of the nonworthless reactions appear on `DF` (what one seeks) but also on `OF`, which must alert us. The reason of this behavior is that the loading of pressure on `OF` was not calculated, because the elements of edge which calculate this loading are not part of the group `STOPPING`.
- Illustration 3 shows that if one calculates `REAC_NODA` on the groups `STOPPING` and `OF`, the reactions are those which one seeks: they are nonworthless only on `DF`. Note: the image seems to show that nonworthless reactions exist on part of `CD` and `FG`, but it is an illusion due to visualization: nodal forces in `D` and `F` "dribble" on the adjacent elements.
- Illustration 4 shows that one should not add too many groups of edge here ( `CD` ). It is seen that nonworthless reactions of supports appear on `CD`. In this case, reaction on the point `D` is false.

#### Conclusion

*If one wants to calculate the reactions of support of the stopping on his foundation, it is necessary to ask the calculation of `REAC_NODA` while specifying exactly **all** meshes of the stopping and **all** meshes of its edge subjected to a loading distributed.  
It is highly advised to visualize the reactions calculated to check that they are nonworthless only on the interface between the stopping and its foundation.*

## 2.10 Calculation of a field user

The keyword factor `CHAM_UTIL` allows to calculate fields unspecified, known as “user” because of the name which will be affected for them in the concept result.

There can be several occurrences of `CHAM_UTIL` in order to connect the calculation of several fields. Treatment being carried out at the end of the order `CALC_CHAMP`, computed fields by the preceding keywords (`CONSTRAINT`, `DEFORMATION...`) are available here.

Either one asks for the calculation of a preset criterion, or one applies one or more formulas to calculate another field.

### 2.10.1 Operand `NOM_CHAM`

It is a question of the field from which the calculations are done. The produced field will have the same type: `ELGA`, `ELNO` or `NOEU`.

### 2.10.2 Operand `CRITERION`

Request the calculation of a preset criterion. The criteria are (the paragraph 2.6.5 provides the expressions of each criterion):

- `VMIS` (for the stress fields),
- `INVA_2` (for the fields of deformations),
- `TRACE` (for the deformation or stress fields).

Each one of these criteria produces a component (named `X1`).

One of the interests is to be able to calculate `INVA_2` of any field of deformations.

### 2.10.3 Operand `FORMULA`

This makes it possible to calculate any expression function of the components of the field provided for `NOM_CHAM`.

The produced field will contain as many components as of provided formulas: to the first formula the component will correspond `X1`, with the second `X2`, etc To 30 components can be thus created.

Examples of formulas allowing to find the criteria `VMIS` and `INVA_2` can be found in the second part of the test `sslv104a`.

### 2.10.4 Operand `NORMALIZES`

Request the calculation of a preset standard. The standards are:

- `L2` : normalizes  $L_2$  of a tensor
- `FROBENIUS` : normalizes of Frobenius of a tensor

The calculated standard is a quantity integrated (with the weak direction) on an element  $\Omega_e$ . For a tensor  $A$ , the standard  $L_2$  is worth:

$$N_{L_2} = \int_{\Omega_e} \sqrt{(A:A)} \cdot d\Omega_e \quad (1)$$

The standard of Frobenius on the components  $A_{ij}$  of a tensor  $A$  :

$$N_F = \int_{\Omega_e} \sum_{i,j} |A_{ij}| \cdot |A_{ij}| \cdot d\Omega_e \quad (2)$$

Each one of these standards produces a component (named X1) on an element. It is thus about one field ELEM. It should be noted that the difference between the two standards comes from the terms cross (except diagonal).

## 2.10.5 Operand NUME\_CHAM\_RESU

The produced field must be arranged, in a single way, in the concept result. The fields "user" are thus numbered while using NUME\_CHAM\_RESU and the type of the field.

The name of the field will be thus of the type UT01\_ELGA, UT22\_NOEU, etc.

## 2.10.6 Example of calculation of a field user

Product the field UT02\_ELGA with two components. X1 is the trace of SIGM\_ELGA (comparable to the component TRSIG of SIEQ\_ELGA) and X2 is the equivalent constraint of Von Mises (component VMIS of SIEQ\_ELGA).

```
fTrace = FORMULA (NOM_PARA= ('SIXX', 'SIYY', 'SIZZ'),
                  VALE= "" SIXX+SIYY+SIZZ "")

fVonMis = FORMULA (NOM_PARA= ('SIXX', 'SIYY', 'SIZZ', 'SIXY', 'SIXZ',
                              'SIYZ'),
                  VALE= "" sqrt (3. /2. * (SIXX ** 2 + SIYY ** 2 + SIZZ **
2
                              + 2*SIXY ** 2 + 2*SIXZ ** 2 + 2*SIYZ ** 2)
                              - 1. /2. * fTrace (SIXX, SIYY, SIZZ) ** 2) "")

LMBO = CALC_CHAMP (reuse=RES,
                  RESULTAT=RES,
                  CHAM_UTIL=_F (NOM_CHAM=' SIGM_ELGA',
                              FORMULE= (fTrace, fVonMis),
                              NUME_CHAM_RESU=2,,))
```

## 2.11 Operand TITLE

◇ TITLE = title

Title which one wants to give to the result of the order [U4.02.01].