

## TTLP101 - Fissured plate at temperatures imposed with condition of exchange through the lips of the crack

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### Summary

This test brings into play a square plate with an emerging right crack, subjected to a variation in temperature. A heat exchange takes place between the lips of the crack (keyword factor `ECHANGE_PAROI` operators `AFFE_CHAR_THER` and `AFFE_CHAR_THER_F` [U4.44.02]).

Three modelings are considered:

- modeling *A* : FEM 2D (crack with a grid)
- modeling *B* : X-FEM 2D , crack in the middle of the elements
- modeling *C* : X-FEM 3D , crack in the middle of the elements

## 1 Problem of reference

### 1.1 Geometry

The structure 2d is a unit square ( $LX=1\text{ m}$ ,  $LY=1\text{ m}$ ), comprising an on the right emerging right crack, located at middle height. (Figure 1.1-a). One calls the line of left the line in  $x=0$ , the line of right-hand side the line in  $x=LX$  and the line the lower line in  $y=0$ .

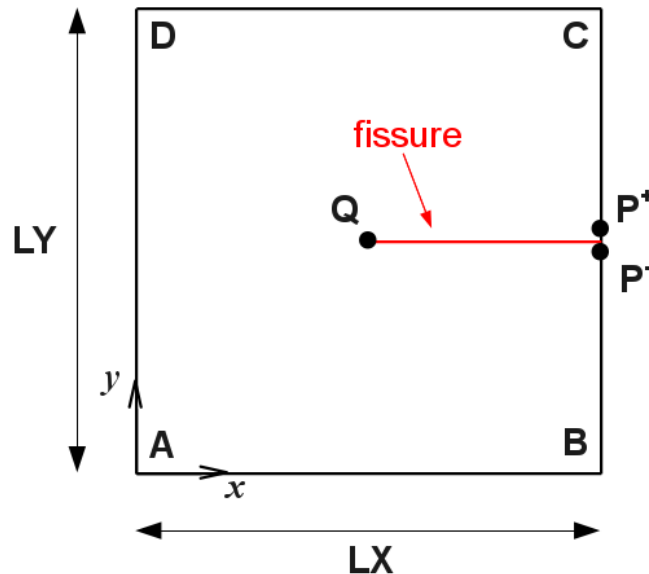


Figure 1.1-a: Geometry of the fissured square plate

One notes  $P^+$  the point of coordinates  $(LX, LY^+/2)$  (located on the upper lip),  $P^-$  the point of coordinates  $(LX, LY^-/2)$  (located on the lower lip), and  $Q$  the point of coordinates  $(LX/2, LY/2)$  (located at a peak of crack).

### 1.2 Properties of material

Thermal conductivity:  $\lambda=1\text{ W.m}^{-1}.\text{K}^{-1}$

Voluminal heat-storage capacity:  $\rho C_p=2\text{ J.m}^{-3}.\text{K}^{-1}$

Coefficient of exchange enters the lips of the crack  $h=2\text{ W.m}^{-2}.\text{K}^{-1}$

### 1.3 Boundary conditions and loadings

One solves the problem on the time interval  $[0.s, 1.s]$  discretized in 5 pas de equal times (of duration  $\Delta t=0.2\text{ s}$ ). One takes the value by default in `THER_LINEAIRE` parameter of the theta-diagram:  $\theta=0.57$ .

On the nodes of the segment  $AB$  (see Figure 1.1-a), one imposes the slope of following temperature:

$$\text{with } t=0.s, \bar{T}^{AB}=10^\circ\text{C}; \quad \text{with } t=1.s, \bar{T}^{AB}=20^\circ\text{C}$$

On the nodes of the segment  $CD$  (see Figure 1.1-a), one imposes the slope of following temperature:

with  $t=0.s$ ,  $\bar{T}^{CD}=20^{\circ}C$  ;      with  $t=1.s$ ,  $\bar{T}^{CD}=40^{\circ}C$

Lastly, on the lips of the crack, one imposes a condition of Neumann of type condition of exchange.

## 1.4 Initial conditions

The initial state is given by solving the stationary problem with  $t=0.s$  (with the boundary conditions given to the paragraph 1.3)

## 2 Reference solution

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### 2.1 Method of calculating

The reference solution is obtained by refining the network of modeling A (elements classical with crack with a grid): regular grid composed of  $500 \times 500$  QUAD4 (instead of  $100 \times 100$  QUAD4 for the grid A)

### 2.2 Sizes and results of reference

One tests the temperature at the end of the last step of time (  $t=1.s$  ) at the points  $P^+$  ,  $P^-$  and  $Q$  (see Figure 1.1-a).

Identification	Type of reference	Value of reference
Not $P^+$ - TEMP	'AUTRE_ASTER'	29.156091860463 °C
Not $P^-$ - TEMP	'AUTRE_ASTER'	23.393394671258 °C
Not $Q$ - TEMP	'AUTRE_ASTER'	26.25259365185 °C

## 3 Modeling A

In this modeling, one considers the structure in 2D . The classical finite element method is used. The crack being with a grid, the condition of exchange between the lips of the crack is applied using the keyword `GROUP_MA1/GROUP_MA2` keyword `factor ECHANGE_PAROI` operators `AFFE_CHAR_THER` and `AFFE_CHAR_THER` [U4.44.02]. This modeling is used as reference for the continuation.

### 3.1 Characteristics of modeling

Modeling is used `PLAN` phenomenon `THERMICS`.

### 3.2 Characteristics of the grid

The structure is modelled by a regular grid composed of  $100 \times 100$  `QUAD8`, respectively along the axes  $x$  and  $y$ . The crack is with a grid.

### 3.3 Sizes tested and results

One tests the temperature at the end of the last step of time (  $t=1.s$  ) at the points  $P^+$  ,  $P^-$  and  $Q$  (see Figure 1.1-a).

Identification	Type of reference	Value of reference	Tolerance
Not $P^+$ - <i>TEMP</i>	'AUTRE_ASTER'	29.156091860463	0.1%
Not $P^-$ - <i>TEMP</i>	'AUTRE_ASTER'	23.393394671258	0.1%
Not $Q$ - <i>TEMP</i>	'AUTRE_ASTER'	26.25259365185	0.5%

## 4 Modeling b: fissures not-with a grid in dimension 2

In this modeling, one considers the structure in 2D . The wide finite element method (X-FEM) is used. The crack not being with a grid, the condition of exchange between the lips of the crack is applied using the keyword `CRACK` keyword factor `ECHANGE_PAROI` of the operator `AFFE_CHAR_THER` [U4.44.02].

### 4.1 Characteristics of modeling

Modeling is used `PLAN` phenomenon `THERMICS`.

### 4.2 Characteristics of the grid

The structure is modelled by a regular grid composed of  $101 \times 101$  `QUAD4`, respectively along the axes  $x$  ,  $y$  . The crack is not with a grid.

### 4.3 Sizes tested and results

One tests the temperature at the end of the last step of time ( $t=1.s$ ) at the points  $P^+$  ,  $P^-$  and  $Q$  (see Figure 1.1-a). For that one tests the field of temperature after call to the operators `POST_MAIL_XFEM` and `POST_CHAM_XFEM`.

Identification	Type of reference	Value of reference	Tolerance
Not $P^+$ - <i>TEMP</i>	'AUTRE_ASTER'	29.156091860463	0.1%
Not $P^-$ - <i>TEMP</i>	'AUTRE_ASTER'	23.393394671258	0.1%
Not $Q$ - <i>TEMP</i>	'AUTRE_ASTER'	26.25259365185	0.5%

## 5 Modeling C: crack not-with a grid in 3D

In this modeling, one considers the structure in 3D. Wide finite element method (X-FEM) is used. The crack not being with a grid, the condition of exchange between the lips of the crack is applied using the keyword `CRACK` keyword factor `ECHANGE_PAROI` of the operator `AFFE_CHAR_THER_F` [U4.44.02].

### 5.1 Characteristics of modeling

Modeling is used 3D phenomenon `THERMICS`.

### 5.2 Characteristics of the grid

The structure is modelled by a regular grid composed of  $11 \times 11 \times 1$  `HEXA8`, respectively along the axes  $x$ ,  $y$  and  $z$ . The crack is not with a grid.

### 5.3 Sizes tested and results

One tests the temperature at the end of the last step of time ( $t=1.s$ ) at the points  $P^+$ ,  $P^-$  and  $Q$  (see Figure 1.1-a). For that one tests the field of temperature after call to the operators `POST_MAIL_XFEM` and `POST_CHAM_XFEM`.

Identification	Type of reference	Value of reference	Tolerance
Not $P^+$ - <i>TEMP</i>	'AUTRE_ASTER'	29.156091860463	0.1%
Not $P^-$ - <i>TEMP</i>	'AUTRE_ASTER'	23.393394671258	0.1%
Not $Q$ - <i>TEMP</i>	'AUTRE_ASTER'	26.25259365185	0.5%

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## 6 Summaries of the results

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The goal of this test is achieved: to validate on a simple case the condition of heat exchange enters the lips of a crack taken into account with the method X-FEM .