

FDLV106 - Computation of damping added out of Summarized

annular flow:

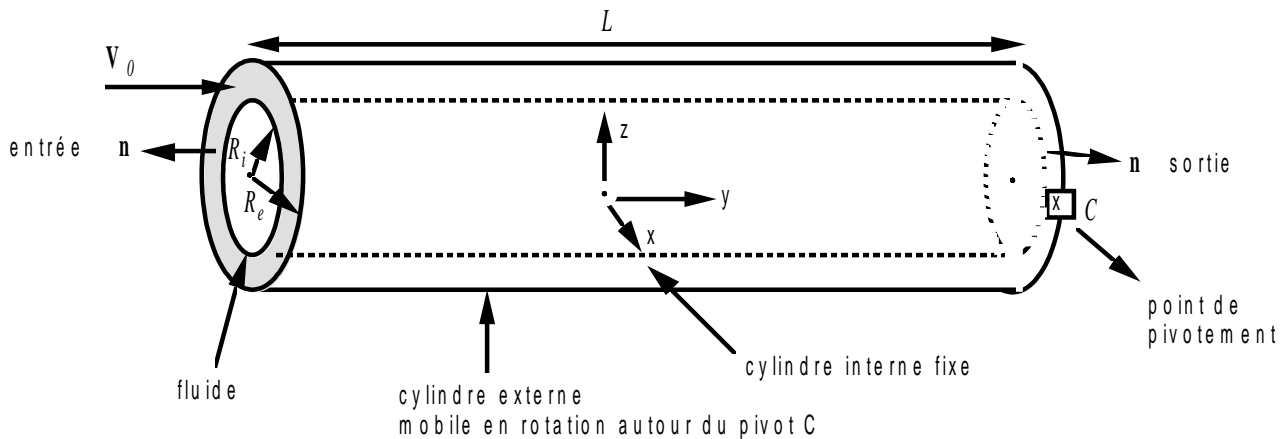
This test of the fluid field/structure implements the computation of mass and damping added on a cylindrical structure subjected to an annular flow which one supposes potential. One calculates mass and damping initially added by flow on the structure for various velocities upstream (4 m/s , 4.24 m/s and 6 m/s), this on a model 3D for the fluid and shell for structure. The structure has a displacement of rotation around a pivot located at the downstream end of the cylinder compared to flow.

The determined coefficients, one assigns them to a discrete model are equivalent to 1 d.o.f. mass-spring-damper, on which one carries out a modal analysis, in order to determine the complex eigenfrequencies of the system for the various rates of flow:

- 4 m/s : damping
- 4.24 m/s : critical velocity, null damping
- 6 m/s : negative damping, undulation.

1 Problem of reference

1.1 Geometry



$$L = 50 \text{ m}$$

$$R_i = 1 \text{ m}$$

$$R_e = 1.1 \text{ m}$$

C : not pivot of external structure

1.2 Properties of the materials

Fluid: density $\rho_g = 1000 \text{ kg/m}^3$ (water).

Structure: $\rho_s = 7800 \text{ kg/m}^3$; $E = 2.10^{11} \text{ Pa}$; $\nu = 0.3$ (steel).

1.3 Boundary conditions and loadings

Fluid:

to simulate steady flow, one forces on the face of entry of the fluid a normal velocity of -4 m/s (by thermal analysis, one imposes a normal heat flux are equivalent of -4),
to compute: the fluid disturbance brought by the motion of the external cylinder Dirichlet in a node of the fluid.

Structure:

one imposes on the external cylinder a displacement of the type $\vec{X}_i = \left(\frac{L}{2} - y\right) \vec{z}$ to the nodes of the mesh of this cylinder.

2 Reference solution

2.1 Method of calculating used for the reference solution

For computation of the added coefficients:

one shows [bib1] that the coefficients of mass and added depreciation depend on the permanent potential fluid velocities $\bar{\phi}$ as well as two fluctuating potentials ϕ_1 and ϕ_2 : these potentials are written in the case of the rotational movement of the external cylinder around the pivot C [bib1]:

$$\begin{cases} \bar{\phi} = V_0 y \\ \phi_1 = \frac{R_e^2}{R_e^2 - R_i^2} \left(r + \frac{R_i^2}{r} \right) \left(y + \frac{L}{2} \right) \sin \theta \text{ avec } \mathbf{X}_i = \left(\frac{L}{2} - y \right) \mathbf{z} \\ \phi_2 = \frac{R_e^2 V_0}{R_e^2 - R_i^2} \left(r + \frac{R_i^2}{r} \right) \sin \theta \end{cases}$$

However the added modal coefficients projected on this mode of rotation are written:

$$M_a = \rho \int_{\text{cylindre externe}} \phi_1 \mathbf{X}_i \cdot \mathbf{n} dS$$

$$C_a = \rho \int_{\text{cylindre externe}} (\phi_2 + \nabla \bar{\phi} \cdot \nabla \phi_1) (\mathbf{X}_i \cdot \mathbf{n}) dS$$

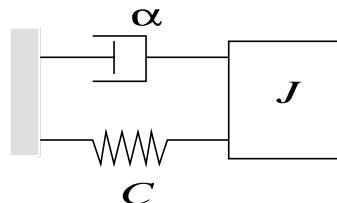
that is to say:

$$C_a = -\rho \frac{V_0 R_e^3 \pi}{R_e^2 - R_i^2} \left(R_e + \frac{R_i^2}{R_e} \right) L^2$$

$$M_a = +\rho \frac{R_e^3}{R_e^2 - R_i^2} \left(R_e + \frac{R_i^2}{R_e} \right) \frac{L^3 \pi}{3}$$

For the system with a degree of freedom are equivalent:

It is about a system mass-spring-damper representing the rotation movement of the cylinder around the pivot C downstream.



the inertia of the mechanical system subjected to flow is written: $J = I + M_a$

where I is the inertia of the external cylinder swivelling compared to the axis Cx (cf appears Ci - below) in air.

It is shown [bib2] that this inertia is worth:

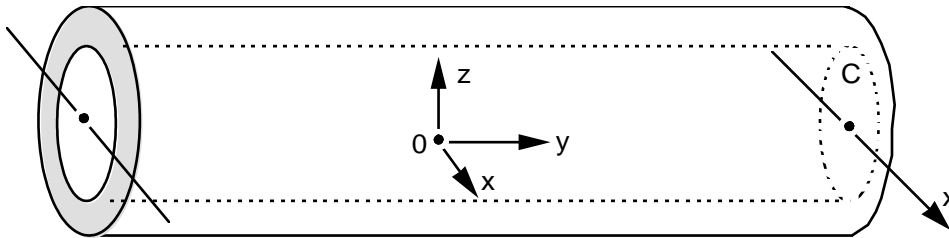
$$I = \frac{m}{6} (3 R_e^2 + 2 L^2)$$

where m is the mass of the cylinder:

$$m = 2 \rho_s \pi R_e e L$$

where e is the thickness of the cylinder, L its overall length.

ρ_s is the density of the cylinder.



$$\text{thus } J = \frac{m}{6} (3 R_e^2 + 2 L^2) + \rho \frac{R_e^3}{R_e^2 - R_i^2} \left(R_e + \frac{R_i^2}{R_e} \right) \frac{L^3 \pi}{3}$$

the damping of the mechanical system subjected to flow is written: $\alpha = A + C_a$

where A is the damping of the mechanical system in air. Usually, A is equal to a few % of the critical damping of the system: $A = 2 \xi \sqrt{IK}$.

where I is the inertia of the cylinder in air calculated above and K the stiffness of spring at the point of swivelling C . One takes reduced damping ξ equal to 1%.

Thus, the total damping of the system under flow is written:

$$\alpha = \xi \sqrt{IK} - \rho V_0 \frac{R_e^3 \pi}{R_e^2 - R_i^2} \left(R_e + \frac{R_i^2}{R_e} \right) L^2$$

the stiffness of the mechanical system subjected to flow is written: $K = K + K_a$

where K is the stiffness of spring in air. K_a is the stiffness added by flow. It is shown [bib1] that this one is null on this mode of rotation.

$$K_a = 0$$

Thus the overall rigidity of the system is independent the rate of flow.

$$K = K$$

One calculates then the complex modes of this mechanical system under flow (damped free vibrations):

$$J \ddot{\theta} + \alpha \dot{\theta} + C \theta = 0$$

The complex eigenfrequencies of this system are written [bib3]:

$$\Omega_{1ou2}^R = -\xi \omega \pm i \omega \sqrt{1 - \xi^2}$$

$$\text{with } \xi = \frac{\alpha}{2J\omega} \quad \text{et} \quad \omega = \sqrt{\frac{K}{J}} = \sqrt{\frac{K}{I + M_a}}$$

ξ : reduced damping of the system

ω : own pulsation.

Numerical applications:

One did three calculations of damping added corresponding to three rates of flow which involve three behavior vibratory of structure:

velocity at 4 m/s
velocity at 4.24 m/s
velocity with 6 m/s

the values of the mechanical system are:

$$e = 2.10^{-2} m \quad L = 50 m \quad R_i = 1 m \quad R_2 = 1,1 m$$

$$I = 4.5 \cdot 10^7 kg \cdot m^2$$

$$A = 4.24 \cdot 10^8 N \cdot m \cdot rad^{-1} \cdot s$$

$$K = 10^{13} N \cdot m \cdot rad^{-1}$$

The added mass and damping brought by flow are worth:

$$I_a = 1.66 \cdot 10^{10} kg \cdot m^2 \quad (\text{independent of the value rate of flow})$$

According to the velocity of entry of the fluid, one a:

| | |
|------------------|---|
| $V_0 = 4 m/s$ | $C_a = -4.00 \cdot 10^8 N \cdot m \cdot rad^{-1} \cdot s$ |
| $V_0 = 4.24 m/s$ | $C_a = -4.24 \cdot 10^8 N \cdot m \cdot rad^{-1} \cdot s$ |
| $V_0 = 6 m/s$ | $C_a = -5.94 \cdot 10^8 N \cdot m \cdot rad^{-1} \cdot s$ |

depreciation of the fluid system/structure is written:

$$\text{with } V_0 = 4 m/s : \alpha = 0.24 \cdot 10^8 N \cdot m \cdot rad^{-1} \cdot s$$

flow does not amplify vibrations. The damping structural intern is sufficiently important to dissipate the energy brought by flow to structure. The system is still damped.

$$\text{with } V_0 = 4.24 m/s : \alpha \approx 0 \quad (\text{vitesse d'écoulement critique})$$

the damping of the system cancels itself.

$$\text{with } V_0 = 6 m/s : \alpha = -1.5 \cdot 10^8 N \cdot m \cdot rad^{-1} \cdot s \quad (\text{l'écoulement amplifie les vibrations})$$

the damping of the system at this last velocity is negative: the system enters then in **flutter instability**.

The reduced dampings corresponding ones are written:

| | |
|--------------------------|--|
| $V_0 = 4 \text{ m/s}$ | $\xi = 1.1 \cdot 10^{-4}$ |
| $V_0 = 4.24 \text{ m/s}$ | $\xi = 0$ (en théorie) $\xi = 1.380 \cdot 10^{-5}$ (avec les erreurs d'arrondi) |
| $V_0 = 6 \text{ m/s}$ | $\xi = -6.6 \cdot 10^{-4}$ |

The own pulsation remains as for it unchanged: $\omega = 12.5 \text{ Hz}$.

2.2 Results of reference

Result analytical.

2.3 References bibliographical

- 1) ROUSSEAU G., LUU H.T. : Mass, damping and stiffness added for a vibrating structure placed in a potential flow - Bibliography and establishment in *the Code_Aster* - HP-61/95/064
- 2) BLEVINS R.D: Formulated for natural frequency and shape mode. ED. Krieger 1984
- 3) SELIGMANN D, MICHEL R: Algorithms of resolution for the quadratic problem [R5.01.02], Handbook of Reference *Aster*.

3 Modelization A

3.1 Characteristic of the modelization

For the system 3D on which one calculates the added coefficients:

| | |
|----------------|--|
| For the fluid: | 480 meshes QUAD4 shell elements MEDKQU4 |
| For solid: | 480 meshes QUAD4 elements thermal THER_FACE4 on cylindrical surfaces 360 meshes thermal QUAD4 elements THER_FACE4 on the sides of entry and output of fluid volume 720 meshes thermal HEXA8 elements THER_HEX8 in fluid annular volume |

3.2 Values tested

| Identification | Reference |
|---------------------------------|-----------------------|
| n°1 Mode | |
| to $V_0 = 4 m/s$ frequency | 12.5 Hz |
| reduced damping | $1.1 \cdot 10^{-4}$ |
| n°1 Mode | |
| with $V_0 = 4.24 m/s$ frequency | 12.5 Hz |
| reduced damping | $1.380 \cdot 10^{-5}$ |
| n°1 Mode | |
| with $V_0 = 6 m/s$ frequency | 12.5 Hz |
| reduced damping | $-6.60 \cdot 10^{-4}$ |

4 Summary of the results

the computational tool of damping under flow (potential assumption) was validated on the mode of rotation of a cylindrical structure subjected to an annular flow. It should however be noted [bib1] that the very good agreement between the model semi-analytical proposed for comparison and numerical computation are obtained only if the cylinder is sufficiently long.

Indeed, the model semi-analytical in fact only one approximate solution of the posed problem is.