

SSNV148 - Weibull models and Rice-Tracey in 3D and discharge

Summarized:

This test of nonlinear quasi-static mechanics makes it possible to validate the Weibull models and of Rice and Tracey in 3D for nonmonotonous cases of mechanical loadings (cf `POST_ELEM`).

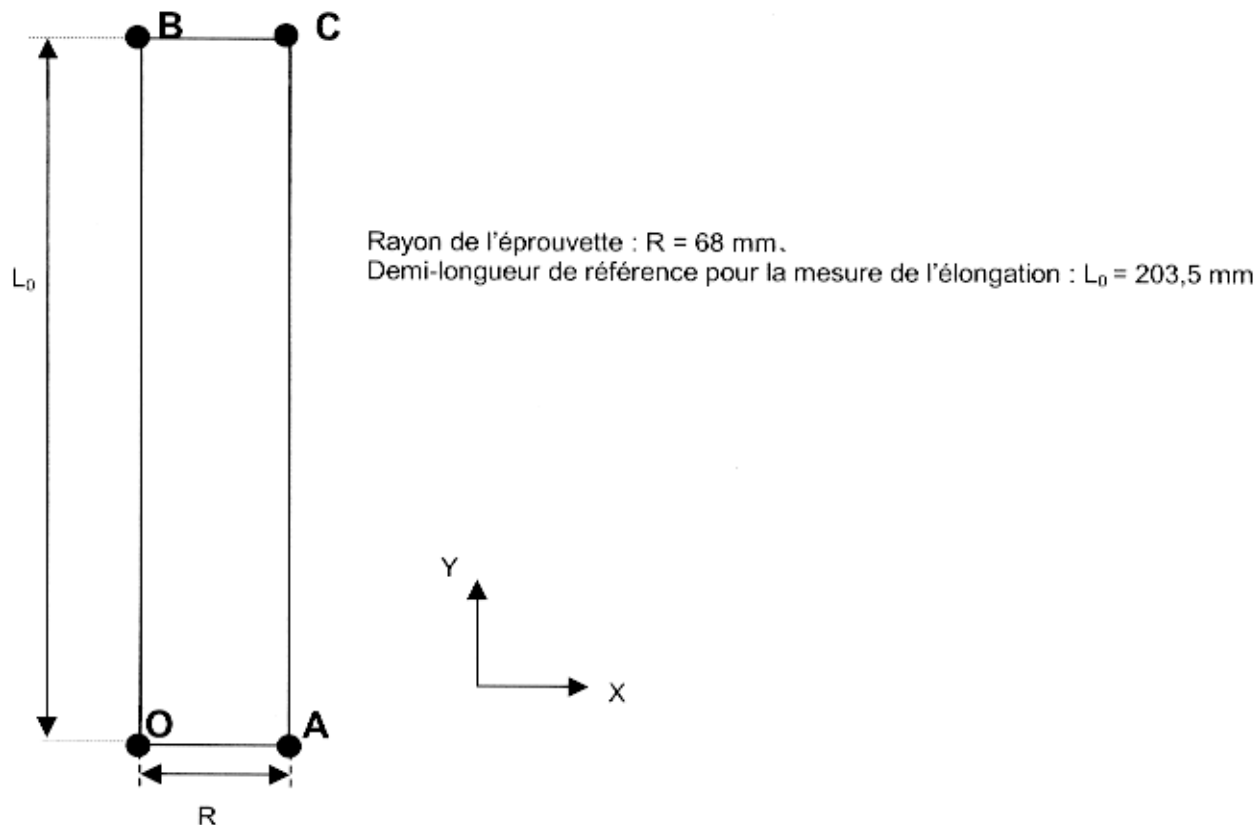
With the temperature of -50°C , a cylindrical test-tube smoothes is first of all deformed up to 10%. After having slightly discharged it, one maintains constant the level of strain reaches while decreasing in a homogeneous way the temperature of the test-tube until -150°C . A this new temperature, one applies an additional strain to reach 15% with the total. The probability of cleavage fracture as well as the growth rate of the cavities of the test-tube are calculated for the group of the way of loading.

The modelization of the test-tube is realized with elements 3D (`HEXA20`, `PENTA15`).

1 Problem of reference

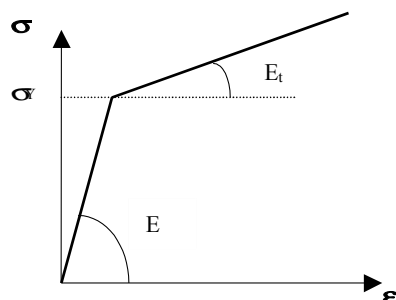
1.1 Geometry

One considers a half - cylindrical test-tube smooth.



1.2 Properties of the material

One adopts an elastoplastic constitutive law of Von Mises with linear isotropic hardening "VMIS_ISOT_LINE". The strains used in the behavior model are the linearized strains.



The Young modulus E , the tangent modulus E_t as well as the Poisson's ratio do not depend on the temperature. One takes: $E = 200 \text{ GPa}$, $E_t = 2000 \text{ MPa}$ and $\nu = 0,3$.

The evolution of the elastic limit with the temperature is given in the following table:

Temperature [$^{\circ}\text{C}$]	- 150	- 100	- 50
$\sigma_Y [\text{MPa}]$	750.700.650		

Lastly, thermal thermal expansion is neglected (thermal coefficient of thermal expansion taken equal to 0).

1.3 Boundary conditions and loadings

While referring to the figure of [§1.1] the boundary conditions are the following ones:

- on surface $SSUP\ BC$ ($Y=L_0$) imposed l displacement following the direction OY ,
- on surface $SINF\ OA$ ($Y=0$) displacements blocked according to the direction OY ,
- displacements of A blocked according to X and Z ,
- displacements of B blocked according to Z .

The evolution temporal of the temperature (presumably homogeneous in the test-tube) and of lengthening l are deferred in the following table:

Times [s]	10	20	30	40
Temperature [°C]	- 50	- 50	- 150	- 150
Displacement $l - L_0$ [mm]	20,35	20,30	20,30	32,525

1.4 Forced

Initial conditions and null strains.

2 Reference solutions

2.1 Method of calculating

In simple tension and with the assumption of the small strains, the stress tensile $\sigma(u)$ as well as the plastic multiplier $\dot{p}(u)$ at time u are given in the case considered by:

- if $0 \leq u \leq t_1^p$: $\sigma(u) = E \frac{l(u) - L_0}{L_0} \dot{p}(u) = 0l(t_1^p) = L_0 \left(1 + \frac{\sigma_Y(-50^\circ C)}{E} \right)$
- if $t_1^p \leq u \leq 10$: $\sigma(u) = E_t \left(\frac{l(u) - L_0}{L_0} \right) + \frac{E - E_t}{E} \sigma_Y(-50^\circ C) \dot{p}(u) = \left(1 - \frac{E_t}{E} \right) \frac{\dot{l}(u)}{L_0}$,
- if $10 \leq u \leq 20$: $\sigma(u) = \sigma(u=10) - E \left(\frac{l(u=10) - l(u)}{L_0} \right) \dot{p}(u) = 0$,
- if $20 \leq u \leq 30$: $\sigma(u) = \sigma(u=20) \dot{p}(u) = 0$,
- if $30 \leq u \leq 40$: $\sigma(u) = \sigma(u=20) + E_t \left(\frac{l(u) - l(u=20)}{L_0} \right) \dot{p}(u) = \left(1 - \frac{E_t}{E} \right) \frac{\dot{l}(u)}{L_0}$

2.2 Weibull

the probability of fracture cumulated P_f at time t is given by (cf POST_ELEM):

$$P_f(t) = 1 - \exp \left(- \sum_{dV} \left(\max_{t^p \leq u \leq t} \left(\frac{\sigma_I(u)}{\sigma_u(\theta(u))} \right)^m \frac{dV}{V_0} \right) \right).$$

The summation relates to the volumes of matter V_i plasticized (from time t_p), $\sigma_I(u)$ and $\theta(u)$ indicating the maximum principal stress and the temperature in each one of these volumes at various times (u). Here, the volume V_0 of reference is equal to $50 \mu m^3$. The modulus of Weibull m is equal to 24 while the stress of cleavage σ_u depends on the temperature according to:

Temperature [$^{\circ}C$]	- 50	- 100	- 150
σ_u [MPa]	2800	2700	2600

the probability of cumulated fracture varies according to $(\theta(t), l(t))$ according to:

$$P_f(t) = 1 - \exp \left(- \left(\max_{t^p \leq u \leq t} \left(\frac{\sigma(u)}{\sigma_u(\theta(u))} \right) \right)^m \frac{V}{V_0} \right).$$

2.3 Rice and Tracey

In simple tension, the Napierian logarithm of the growth rate of the cavities at time t is given by (cf POST_ELEM):

$$\text{Log} \left(\frac{R(t)}{R_0} \right) = 0,283 \times \exp(0,5) \times \int_0^t \dot{p}(u) du$$

2.4 Quantities and results of reference

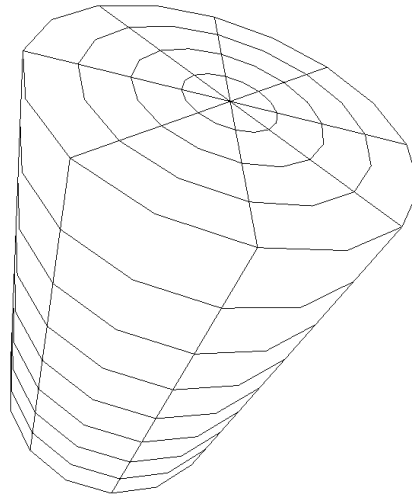
P_f and $\frac{R}{R_0}$ for the couples (temperature, displacements = $(l-l_0)$) following:
 $(-50,0^{\circ}C, 20,35 \text{ mm})$;
 $(-50,0^{\circ}C, 20,30 \text{ mm})$; $(-150,0^{\circ}C, 20,30 \text{ mm})$ and $(-150,0^{\circ}C, 32,53 \text{ mm})$.

2.5 Uncertainties on the analytical

solution Solution.

3 Modelization A

3.1 Characteristic of the mesh



Many nodes: 1137
Number of meshes and types: 64 (PENTA15), 192 (HEXA20)

3.2 Quantities tested and results

$T [^{\circ}C]$	$l - L_0 [mm]$	Reference			Code_Aster		
		P_f	P_f	% diff.	$\frac{R}{R_0}$	$\frac{R}{R_0}$	% diff.
- 50	20,35	0,01465	0,01481	1,1	1,0447	1,0458	0,1
- 50	20,30	0,01465	0,01481	1,1	1,0447	1,0458	0,1
- 150	20,30	0,01465	0,01481	1,1	1,0447	1,0458	0,1
- 150	32,525	1,0,1,0,0, 0			1,068	1,0701	0,2

4 Summary of the results

the results got by Code_Aster are very close to the analytical solutions of reference.