

---

## SDNS01 - Model probabilistic nonparametric - parametric of a flexbeam with nonlocalised linearities of Summarized

---

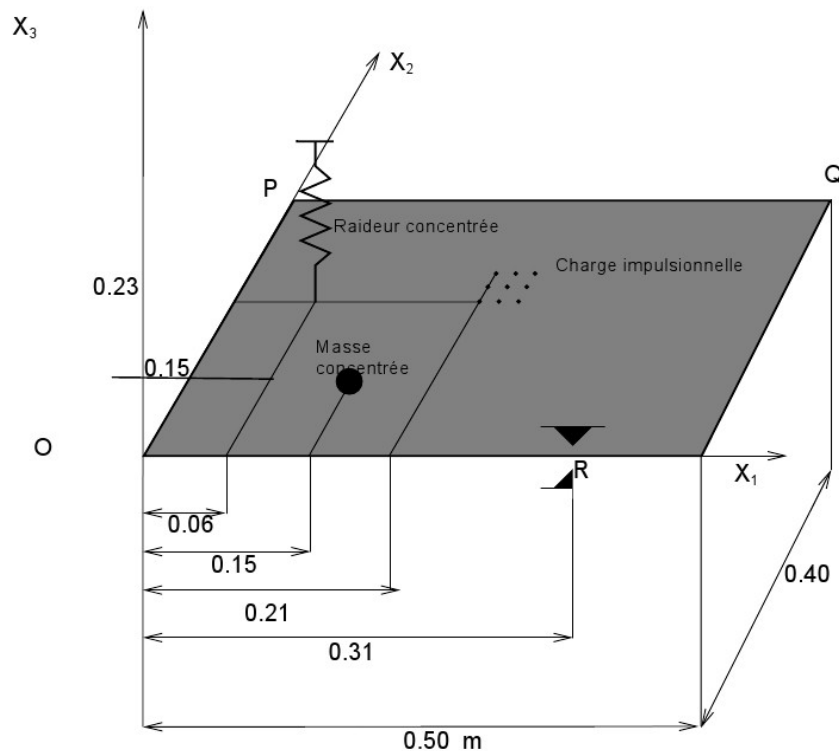
### shock:

This benchmark relates to the nonparametric and parametric probabilistic models of uncertainties in linear dynamics with possibly of nonthe localised linearities. The model mechanical used is a rectangular plate with an elastic thrust of shock. The random generators of matrixes and random variables (operators `GENE_MATR_ALEA` and `GENE_VARI_ALEA`) are tested and validated in this case test. Statistical postprocessings (`CALC_FONCTION`) are also tested.

This benchmark has two modelizations. The first uses a proportional damping. The second uses a reduced damping defined by the key word `CALC_AMOR_GENE` of `COMB_MATR_ASSE` testing this functionality thus.

## 1 Problem of reference

### 1.1 Geometry



Thickness of the plate:  $e = 0.0004 \text{ m}$ .

Clearance enters the thrusts :  $jeu = \pm 0.002 \text{ m}$ .

### 1.2 Material properties

#### Plates:

Poisson's ratio: 0.3

Young modulus:  $2.1 \cdot 10^{11} \text{ N/m}^2$

Density:  $7800 \text{ kg/m}^3$

Concentrated stiffness:  $2.388 \cdot 10^7 \text{ N/m}$

Lumped mass:  $4 \text{ kg}$

Stiffness of shock:  $25000 \text{ N/m}$

### 1.3 Boundary conditions and loadings

the flexbeam is out of simple on 3 edges and free bearing on its fourth edge OR. The blocked degrees of freedom are thus:

- on  $OP$  and  $QR$ , displacements according to  $X_1, X_2, X_3$  and the rotations according to  $X_1, X_3$ .
- on  $PQ$ , displacements according to  $X_1, X_2, X_3$  and the rotations according to  $X_2, X_3$ .

*Warning : The translation process used on this website is a "Machine Translation". It may be imprecise and inaccurate in whole or in part and is provided as a convenience.*

• on OR , déplacements according to  $X_1, X_2$  .

The plate is subjected to a vertical impulse load  $e(t)$  on 9 nodes of the plate according to the direction  $X_3$  . The loading  $e(t)$  is such that, for  $t < 0$  and  $t > 2t_1$  ,  $e(t) = 0$  and for  $0 \leq t \leq 2t_1$  :

$$e(t) = (\Delta\omega(t-t_1))^{-1} (\sin((\Omega_c + \Delta\omega/2)(t-t_1)) - \sin((\Omega_c - \Delta\omega/2)(t-t_1))) .$$

with  $t_1 = 2\pi/\Delta\omega$   $\Delta\omega = 2\pi \times 40 \text{ rad/s}$   $\Omega_c = 2\pi \times 20 \text{ rad/s}$  .

The energy of the function  $e(t)$  is mainly distributed in the frequential tape  $[0,60] \text{ Hz}$  , which contains 8 elastic modes of the linearized dynamic system.

## 1.4 Initial conditions

the dynamic system is initially at rest.

## 2 Reference solution

---

### 2.1 Method of calculating used for the reference solution

We on the structure study the transient response of a nonlinear dynamic system subjected to a deterministic impulse load due to a shock. Nonthe linearity of the system is due to an elastic thrust of high stiffness comprising a certain clearance. The response spectrums in frequency standardized are used in order to study the transient response of this system. The equations of the dynamics are discretized by the method with the finite elements. The mesh of structure is supposed sufficiently fine to collect all the dynamic phenomena of this mechanical system in term of field of displacement for the impulse loading considered. Random uncertainties of the dynamic system are modelled by means of the model probabilistic nonparametric uncertainties. Consequently, the transient response is a nonsteady stochastic process whose statistical estimates are evaluated.

The results of reference are given in the form of graphs in the article referred below, consultable on <http://www.resonance-pub.com>.

### 2.2 Bibliographical reference

1.C. SOIZE: Not linear dynamical Systems with Nonparametric Model of Random Uncertainties”, *Uncertainties in Engineering Mechanics* (2001) 1(1), 1-38, <http://www.resonance-pub.com> Modelization

## 3 A Characteristic

### 3.1 of the modelization Modelization

: DKT The model

average with the finite elements of the plate consists of a regular rectangular mesh whose step is constant and is worth in 0.01m the directions and  $X_1$  .  $X_2$  There are thus 41 nodes in the width and 51 nodes in the length. Consequently, all the finite elements are identical and each one is an element plates with 4 nodes. This model finite elements layer comprises 2000 finite elements and degrees of freedom  $m=6009$  , by counting only the translations in and the  $z$  rotations according to and  $X_1$  ).  $X_2$

The eigenfrequencies of the linearized dynamic system (the plate without the thrusts of shock but with the masses and stiffness concentrated) are: .

$$f_1=1.94, f_2=10.28, f_3=15.47, \dots, f_8=53.5, f_9=66.1, f_{10}=68.9, \dots, f_{30}=198.3, \\ f_{31}=206.0, f_{32}=208.9, \dots, f_{50}=330.9, f_{51}=336.3, \dots, f_{100}=670.8, f_{120}=817.6\text{Hz Modeliza}$$

tion

: DIS\_T

the lumped masses and the concentrated stiffness are modelled by elements DIST \_T. Damping

the damping matrix of  $[D]$  the model average finite element is defined as being a linear combination of the matrixes finite elements averages of mass and  $[M]$  stiffness.  $[K]$  One thus has with  $[D]=a[M]+b[K]$  and

$$a = \frac{2\xi\Omega_{max}\Omega_{min}}{\Omega_{max} + \Omega_{min}} \text{ where } b = \frac{2\xi}{\Omega_{max} + \Omega_{min}}$$

,  $\xi=0.04$  and  $\Omega_{min}=4\pi \text{ rad/s}$  .  $\Omega_{max}=200\pi \text{ rad/s}$  Scale model

#### and degree of freedom observed For

this case test, the model finite elements is linearized project on the first 5 elastic modes of structure, which constitutes the data of the average scale model. It should be noted that the first 5 modes are not enough to obtain convergence compared to the number of modes (cf paragraph Comments of the results of the modelizations).

The degree of freedom observed is the degree of freedom corresponding  $j_{stop}$  to following displacement in translation of  $z$  the node or are the elastic thrusts. It is the node of coordinates. (0.31, 0, 0) The response sprectrum standardized for this degree of freedom is built for a tape of frequential analysis and  $J=2\pi[1, 100]\text{rad/s}$  of which the frequential resolution is of. 0.5Hz Achievements

#### of the random matrixes of the nonparametric probabilistic model – parametric

the mass matrixes, of stiffness and dissipation of the scale model layers are replaced by achievements of the random matrixes of mass, stiffness and of nonparametric dissipation following the model probabilistic. For that, we use the generator of random matrixes GENE \_MATR\_ALEA. During the first call to this generator, key word INIT must take the value "YES" in order to

initialize the generator of random variable of uniform model of Python. Thereafter, INIT will be able to take its default value (INIT= 'NON'). The initialization of the generator of random variable of Python is to be done only one and only once by study, in theory, except if the user explicitly wishes to re-use the same sequence random pseudonym.

The level of dispersion of the random matrixes of the nonparametric probabilistic model is controlled by a parameter of dispersion built-in  $\delta$  to 20% ().  $\delta=0.2$  Key word DELTA thus takes value 0.2. Lastly,

for each pulling of the random matrixes of mass, stiffness and dissipation, it is necessary to inform the corresponding average matrix of the model reduces average via key word MATR\_MOYEN .

The stiffness of shock is also made random due to uncertainties. To build a realization of the stiffness of shock following a model gamma, we use random generator GENE\_VARI\_ALEA with the key word TYPE = 'GAMMA'. We suppose that possible all the values for the achievements of the random stiffness of shock are the interval,  $[0, +\infty[$  that the mean value of all the achievements of the stiffness of shock corresponds to the stiffness of shock of the model finite elements layer. The level of dispersion of the achievements of the stiffness of shock is controlled by a parameter built-in  $\delta$  to 1% ().  $\delta=0.01$  Key word DELTA thus takes the value. 0.01 Resolution

## of the probabilistic nonlinear dynamic system.

Operator DYNA\_VIBRA is used to build the transient response of the nonlinear dynamic system for each realization of the random stiffness of random shock and the matrixes of mass, stiffness and dissipation. It should be noted that we carry out for this case test only achievements  $n_s=5$  of each random variable (stiffness of shock + matrixes) what corresponds to 5 iteration of the method of computational simulation of Monte Carlo (cf paragraph Comments of the Results of the modelizations).

The temporal interval of the study is,  $T=[0,4]_s$  with a step of.  $5 \cdot 10^{-5}_s$  The diagram of temporal integration selected is EULER . Construction

## of the statistical estimates. After

each call to DYNA\_VIBRA, we have a realization of the stochastic process of generalized displacements. It is thus possible to build acceleration with the node of shock following the degree of freedom by the operator  $j_{stop}$  RECEIVED\_FONCTION. The standardized response spectrum is then built by the operator CALC\_FONCTION. These

two operations are classically carried out during deterministic studies and give us here a realization of the stochastic process of the standardized response spectrum. It is then a question of building statistical estimates of the achievements  $n_s$  of this last. The estimates under consideration in this case test are the envelopes min and max as well as the average and the moment of order two of the standardized response spectrums. A each pulling (iteration of Monte Carlo) we build these estimates with the assistance only of operator CALC\_FONCTION and key words ENVELOPPE , PUISSANCE and COMB . At the end of the iterations  $n_s$  of Monte Carlo, we have the required statistical estimates relating to the stochastic process of the standardized response spectrum. Finally the norm of  $L2$  the average is calculated by the key word NORMALIZES of operator CALC\_FONCTION. The interest to evaluate such a norm is to allow studies of convergence according to the number of modes of the random average scale model and according to the iteration count of the numerical method of Monte Carlo. This norm is calculated here to check that the functionality goes, but convergence is not reached to save the TEMPS CPU. Characteristics

## 3.2 of the mesh Many

degrees of freedom: 6009 Many

finite elements: 2000 QUA4 and 2 DIS\_T Quantities

### 3.3 tested and results

the initial validity of the case test was established by comparison with bibliographical reference given in [§3.2]. One

tests the following values into non regression (cf comments): Statistics

---

**on the values of the response spectrum with 50Hz with the degree of freedom observed (cf modelization) Identification**

---

| References   | Estimate      |
|--|---------------|
| of the envelope max 4.4433958494950                | E+02 Estimate |
| of the envelope min 1.2534278720661                | E+02 Estimate |
| of the average 3.2330416710925                     | E+02 Estimate |
| of the moment of order 2 1.2260792008492           | E+02 Estimate |
| of the Norm of $L2$ the average<br>2.0657959602609 | E+03 Comments |

### 3.4

the various statistical estimates are not converged here. Only 5 simulations of Assembles - Carlo were made. One would have needed 700 at least of them. Moreover, it is necessary to increase the number of modes with 50 to obtain the convergence of the model project in the waveband considered. Computations being then too long for a case test, we preferred to voluntarily degenerate two convergences after validation of those on a complete study. After convergence, the statistical estimates calculated from Aster *correspond* very exactly to the results given by the standard commodity. Modelization

## 4 B Characteristic

---

### 4.1 of the modelization Only

the modelization of damping changes modelization A. Amortissement compared to the

damping matrix of  $[D]$  the model average finite element is defined as corresponding with a straight line modal reduced damping of 4%. Characteristics

### 4.2 of the mesh Many

degrees of freedom: 6009 Many  
finite elements: 2000 QUA 4 and 2 DIS\_T Quantities

### 4.3 tested and results One

tests the following values into non regression, with: 50Hz Statistics

---

**on the values of the response spectrum with to 50Hz the degree of freedom observed (cf modelization) Identification**

---

| References                                      | Estimate      |
|---|---------------|
| of the envelope max 2.7570639015302             | E+02 Estimate |
| of the envelope min 9.3629561795277             | E+01 Estimate |
| of the average 1.9641139264813                  | E+02 Estimate |
| of the moment of order 2 4.3869049613023        | E+04 Estimate |
| of the Norm of $L2$ the average 1.2384277999571 | E+03 Comments |

### 4.4 Same

comments as for modelization A. Synthèse

## 5 of the results

---

the got results are completely in conformity with those of bibliographical reference [§2.2] entirely obtained in Matlab.