

TTNL100 – Nonlinear thermal source, homogeneous solution in Summarized

space:

This test checks thermal computation in the presence of a loading of nonlinear source, depend on the temperature.

The reference solution is analytical. The part considered in the two modelizations is a single element:

- an element TRIA3 for a modelization planes
- an element PENTA6 for a modelization 3D

the temperature being homogeneous in the element, computation can be regarded as 0D.

1 Problem of reference

1.1 Geometry

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1.2 Properties of the thermal

$\lambda = 0$ material conductivity
 $\rho C = 2$ voluminal heat

1.3 Boundary conditions and loadings

nonlinear Loading of volumic source, function of the temperature:

$$s(T) = 2 - 2 \times w \times T \text{ with } w = 2$$

the boundary conditions are adiabatic, which corresponds to the default in *Code_Aster* .

The temporal beach $[0.; 1.]$ is discretized into 100 time step (lasted of each time step equalizes with 0.01).

1.4 Initial conditions

$T0 = 0$ in all the element.

2 Reference solution

2.1 Method of calculating used for the reference solution

In this problem, the boundary conditions are adiabatic, the initial temperature is constant equal to T_0 and the loading is tiny room to the function heat source of the temperature $r(T) = r_0 - r_1 T$ where r_1 is positive for questions of thermal stability. These conditions ensure well a homogeneous solution in space. The equation of heat is reduced to:

$$\rho C_p \dot{T} = r_0 - r_1 T ; T(0) = T_0 \quad [\text{éq1}]$$

By standardization, one can be reduced without loss of generality to the following equation:

$$\dot{u} = 1 - \omega u ; u(0) = 0 \quad [\text{éq2}]$$

the solution of this first order differential equation is then:

$$u(t) = \frac{1}{\omega} (1 - e^{-\omega t})$$

Rather than to go up u solution of [éq2] with T solution of [éq1], one prefers to adopt the set of following parameters, without lending guard to the units, which leads to $T = u : T_0 = 0$, $r_0 = \rho C$ and $r_1 = \omega r_0$.

2.2 Results of reference

the benchmark is carried out with $\omega = 2$ and one examines the temperature with $t = 1$ in an unspecified node of the element. The data are the following ones:

Thermal conductivity	LAMBDA0	.
Voluminal heat capacity	RHO_CP	2.
Initial temperature	T_0	0.
Heat source	r_0 r_1	2. 4.

Quantity tested	$T (t = 1)$
Value of reference	0.432 332

3 Modelization A

3.1 Characteristic of the modelization

The mesh of this modelization is composed of a single element TRIA3 in modelization PLANE , whose dimensions do not import since the solution is homogeneous in space.

4 Results of the modelization A

4.1 Values tested

the solution is in conformity with the analytical value with less than 0.05 %.

5 Modelization B

5.1 Characteristic of the modelization

The mesh of this modelization is composed of a single element PENTA6 in modelization 3D , whose dimensions do not import since the solution is homogeneous in space.

6 Results of the modelization B

6.1 Values tested

the solution is in conformity with the analytical value with less than 0.05 %.

7 Summary of the results

the results are in conformity with the analytical solution.