

SSLS122 - Rectangular isotropic homogeneous plate offset

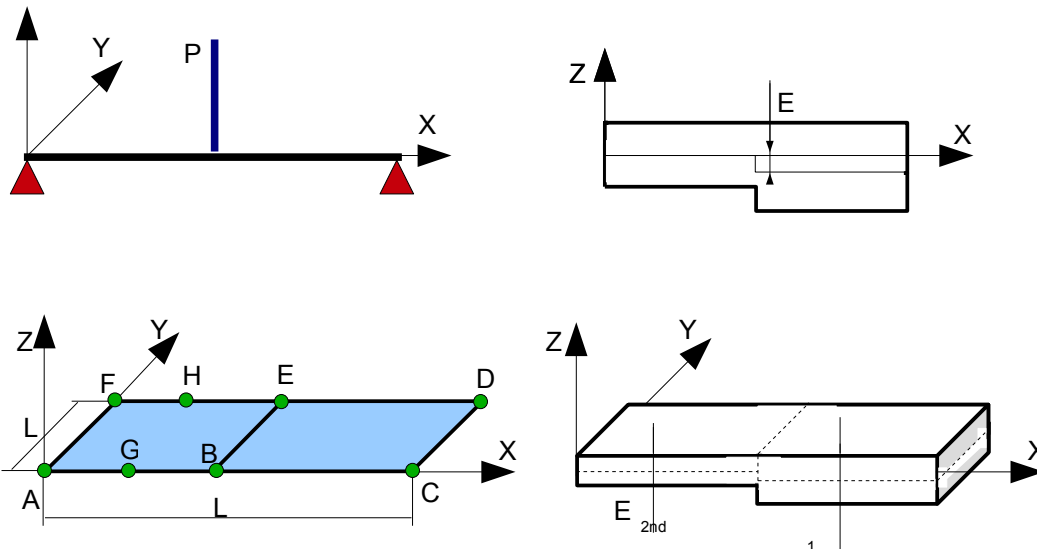
Summarized:

This benchmark makes it possible to test the eccentricity of the plates with modelizations `DKT` and `DST`.

1 Problem of reference

1.1 Geometry

Bending 3 points



Characteristic of the plates (m) :

Length: $L=10$

Width: $l=1$

Thickness 1: $e_1=0.1$

Thickness 2: $e_2=0.08$

Eccentring: $e=0.01$

Coordinates of the points (m) :

$A:(0,0)$	$E:(5,1)$
$B:(5,0)$	$F:(0,1)$
$C:(10,0)$	$G:(2.5,0)$
$D:(10,1)$	$H:(2.5,1)$

1.2 Properties of the Elastic

material

- $E=2.1 \times 10^{11} Pa$ Modulus Young
- $\nu=0.3$ Poisson's ratio

1.3 Boundary conditions and loadings

imposed Displacement (m) :

- segment AF, CD : $DZ=0$
- segment FA : $DX=0$
- point: A : $DX=DY=DRZ=0$

Loading

- Pressure on BE : $p=2.\times 10^5 N/m$ $P=pl$

2 Reference solution

2.1 Method of calculating used for the reference solution

Displacements:

- Points B and E

$$f = \frac{Pl^3}{96EI_1} + \frac{Pl^3}{96EI_2} \text{ with } I_i = \frac{b \times e_i^3}{12}$$

- Points G and H

$$f = -\frac{Pl^3}{192EI_1} \left(\frac{I_1}{I_2} + \frac{7}{2} \right)$$

- Bending moment:

$$M(x) = \frac{P \cdot x}{2}$$

2.2 Reference variable

- DZ displacement following z to the points B and G .
- MXX bending moment for $x = \frac{L}{2}$ and $x = \frac{L}{4}$

2.3 Quantity and result of reference

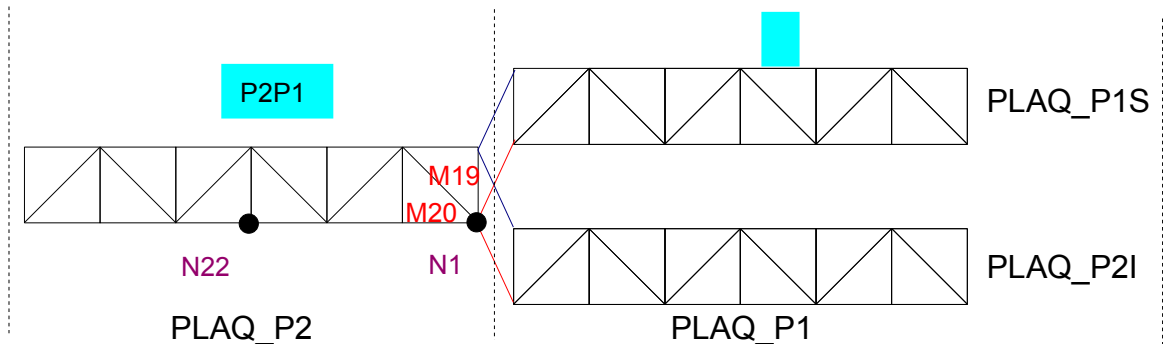
Not	Component	Reference
B	DZ	0.3515625 m
	DRZ	0.
	MXX	$-50 \times 10^4 \text{ m.N}$
G	DZ	-0.2629743 m
	DRZ	0.
	MXX	$-25. \times 10^4 \text{ m.N}$

3 Modelization A

3.1 Characteristic of the modelization A

The mesh of the plate is composed in two parts:

- *P1* , constituted of a nonexcentré mesh
- *P2* , made up by two superimposed meshes:
 - *PLAQ_P1S* excentré of 0.015m
 - *PLAQ_P1I* excentré of -0.035m



Modelization DKT:

Many nodes	26	Are:	SEG2	3
Number of meshes	39		TRIA3	36

Nodes group:

- *A, B, C, D, E, F, G, H*

Mesh group:

- *PLAQUE* : surface *ACDF*
- *PLAQ_P1* : surface *BCDE*
- *PLAQ_P2* : surface *ABEF*
- *CD* : segment *CD*
- *FA* : segment *FA*
- *BE* : segment *BE*

3.2 Result of the modelization A

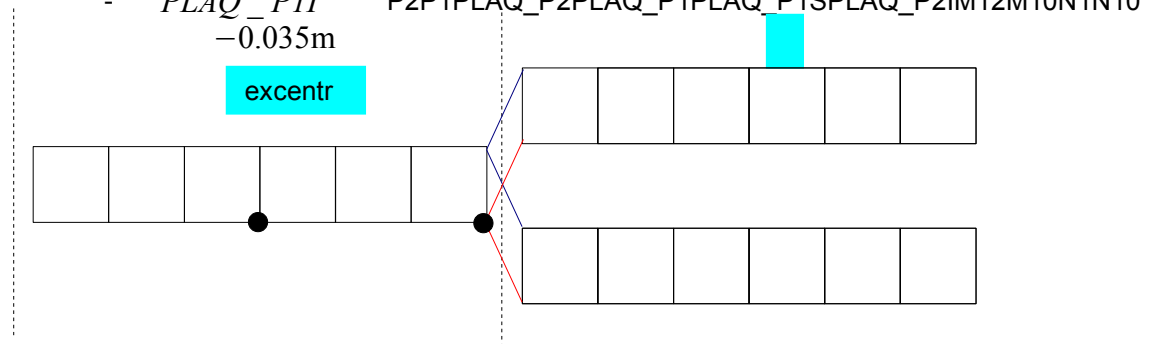
Not	Mesh	node	Component	Reference	Tolerance (%)
<i>B</i>		<i>N1</i>	<i>DZ</i>	0.3515625 m	1.
		<i>N1</i>	<i>DRZ</i>	0.	0.1
		<i>M19</i>	<i>MXX</i>	-500 000. m.N	3.
		<i>M20</i>	<i>MXX</i>	-500 000. m.N	5.
<i>G</i>		<i>N22</i>	<i>DZ</i>	-0.2629743 m	1.
		<i>N22</i>	<i>DRZ</i>	0.	0.1

4 Modelization B

4.1 Characteristic of the modelization B

The mesh of the plate is composed in two parts:

- $P1$, constituted of a nonexcentré mesh
- $P2$, made up by two superimposed meshes:
 - $PLAQ_PIS$ excentré of 0.015m
 - $PLAQ_PII$ P2P1PLAQ_P2PLAQ_P1PLAQ_P1SPLAQ_P2IM12M10N1N10 of -0.035m



Modelization DKT:

Many nodes 26
Number of meshes 21
Are: SEG3 3
QUAD4 18

Nodes group:

- A, B, C, D, E, F, G, H

Mesh group:

- $PLAQUE$: surface $ACDF$
- $PLAQ_P1$: surface $BCDE$
- $PLAQ_P2$: surface $ABEF$
- CD : segment CD
- FA : segment FA
- BE : segment BE

4.2 Result of the modelization B

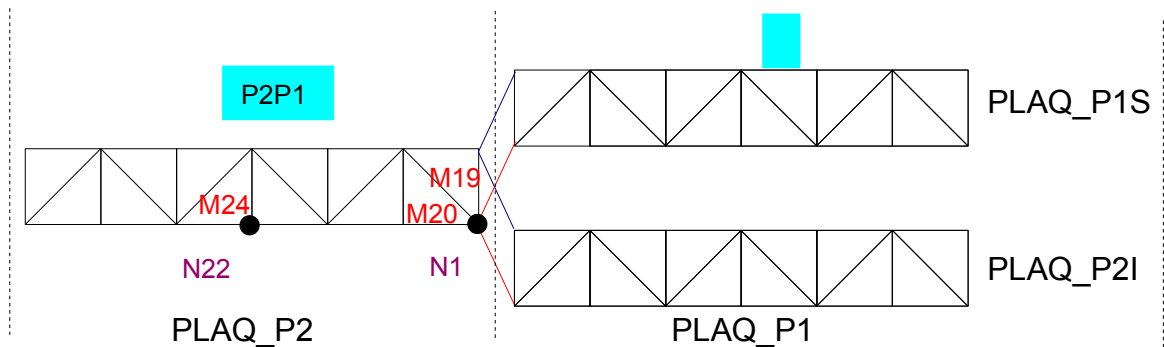
Not	Mesh	node	Component	Reference	Tolerance (%)
B		N1	DZ	0.3515625 m	1.
		N1	DRZ	0.	0.1
	M12	N1	MXX	-500 000. m.N	0.1
G		N10	DZ	-0.2629743 m	1.
		N10	DRZ	0.	0.1
	M10	N10	MXX	-250 000. m.N	0.1

5 Modelization C

5.1 Characteristic of the modelization C

The mesh of the plate is composed in two parts:

- $P1$, constituted of a nonexcentré mesh
- $P2$, made up by two superimposed meshes:
 - $PLAQ_P1S$ excentré of 0.015m
 - $PLAQ_P1I$ excentré of $-0.035m$



Modelization DST:

Many nodes	26			
Number of meshes	39	Are:	SEG3	3
			TRIA3	36

Nodes group:

- A, B, C, D, E, F, G, H

Mesh group:

- $PLAQUE$: surface $ACDF$
- $PLAQ_P1$: surface $BCDE$
- $PLAQ_P2$: surface $ABEF$
- CD : segment CD
- FA : segment FA
- BE : segment BE

5.2 Result of the modelization C

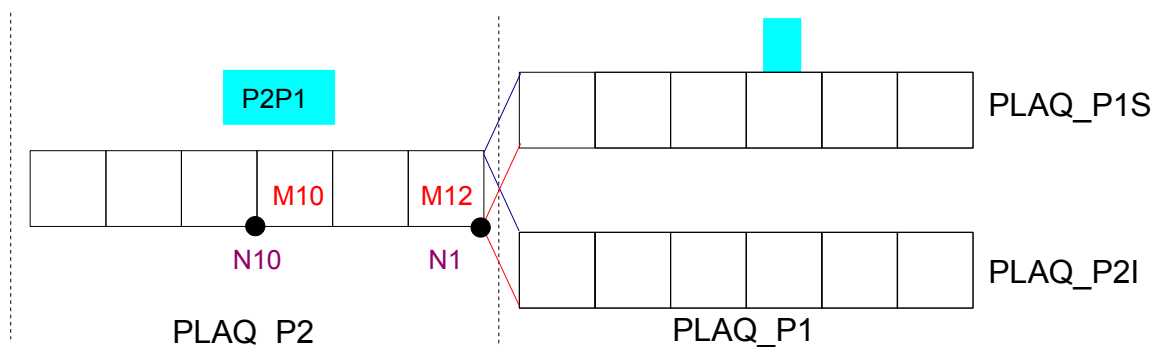
Not	Mesh	node	Component	Reference	Tolerance (%)
B		N1	DZ	0.3515625 m	0.5
		N1	DRZ	0.	0.1
	M19	N1	MXX	-500 000. m.N	2.
G		N22	DZ	-0.2629743 m	0.5
		N22	DRZ	0.	0.1
	M22	N22	MXX	-250 000. m.N	13.

6 Modelization D

6.1 Characteristic of the modelization D

The mesh of the plate is composed in two parts:

- $P1$, constituted of a nonexcentré mesh
- $P2$, made up by two superimposed meshes:
 - $PLAQ_P1S$ excentré of 0.015m
 - $PLAQ_P1I$ excentré of -0.035m



Modelization DST :

Many nodes	26			
Number of meshes	21	Are:	SEG3	3
			QUAD4	18

Nodes group:

- A, B, C, D, E, F, G, H

Mesh group:

- $PLAQUE$: surface $ACDF$
- $PLAQ_P1$: surface $BCDE$
- $PLAQ_P2$: surface $ABEF$
- CD : segment CD
- FA : segment FA
- BE : segment BE

6.2 Result of the modelization D

Not	Mesh	node	Component	Reference	Tolerance (%)
B		$N1$	DZ	0.3515625 m	0.4
		$N1$	DRZ	0.	0.1
	$M12$	$N1$	MXX	-500 000. m.N	0.1
G		$N10$	DZ	-0.2629743 m	0.4
		$N10$	DRZ	0.	0.1
	$M10$	$N10$	MXX	-250 000. m.N	0.1

7 Summary of the results

the got results are satisfactory.