

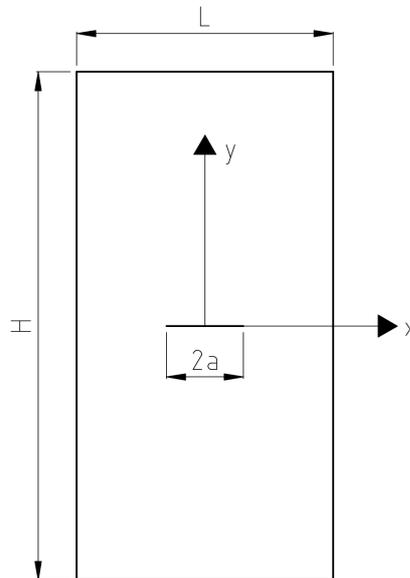
SSLP318 - Propagation of a crack X-FEM not emerging solicited in mode I

Summarized:

The goal of this test is to check that operator `PROPA_FISS` treats the cases of multi-cracking correctly. It is about a plate `2D` containing only one crack made up of two crack tips. Several propagations are calculated by the operator `PROPA_FISS`. It is checked that the factors of intensity of the stresses of propagated crack are correct for a propagation in mode `I`.

1 Problem of reference

1.1 Geometry



Appears 1.1-a: geometry of the fissured plate

geometrical Dimensions of the fissured plate:

width $L = 1000 \text{ mm}$
height $H = 2000 \text{ mm}$

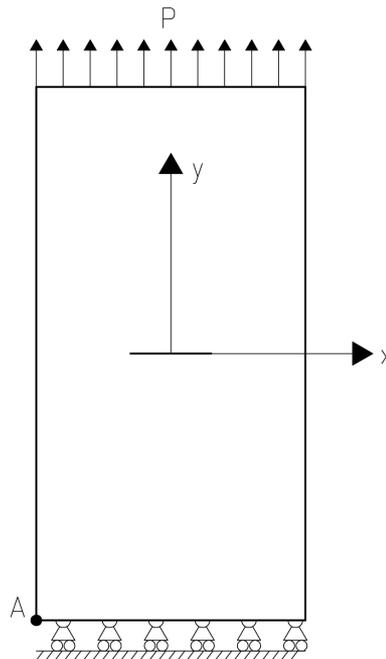
initial Length of crack: $2a_0 = 300 \text{ mm}$.

The crack is positioned in the middle of the height of the plate ($H/2$).

1.2 Properties of the material

Young's modulus $E = 206000 \text{ MPa}$
Poisson's ratio $\nu = 0.33$

1.3 Boundary conditions and loadings



Appears 1.3-a: boundary conditions and loadings

Boundary conditions:

Point: $A \quad \Delta X = \Delta Y = 0$

Points of the lower end of the plate: $\Delta Y = 0$

Loading:

Pressure applied at the higher end of the plate: $P = 1 \text{ MPa}$

Three propagations are calculated by imposing an advance of crack equal on 30 mm to the level of each crack tip. As a consequence of the symmetry of the geometry, boundary conditions and loading, the advances of the two funds of crack are always equal in advance imposed.

2 Reference solution

2.1 Method of calculating

Three propagations of crack are calculated. The two funds of crack always advance same distance and their factors of intensity of the stresses are always equal between them.

One can by means of calculate the factors of intensity of the stresses the following equations [bib1]:

$$K_I = -P \cdot \sqrt{\pi \cdot a \cdot \left(\cos\left(\frac{\pi a}{L}\right) \right)^{-1}}$$
$$K_{II} = 0$$

2.2 Quantities and results of reference

For the three propagations calculated in the tests, the half-length of crack is the following one:

Propagation	has [mm]
1	180.0
2	210.0
3	240.0

Table 2.1

the value of K_I expected is thus the following one for each propagated bottom:

Propagation	K_I [Pa \sqrt{mm}]
1	2.2997E+07
2	2.5878E+07
3	2.8894E+07

Table 2.2

the value of K_{II} expected is always equal to zero.

2.3 Bibliography

[1] D.Broek, "Elementary engineering A fractures mechanics", Martinus Nijhoff Publishers, The La Hague, The Netherlands,

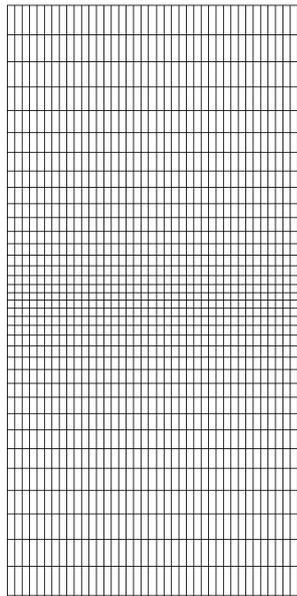
3 1982 Modelization

3.1 Characteristic of the modelization

method UPWIND is used by PROPA_FISS to solve the equations of propagation of crack. No auxiliary grid is used. That is possible because the mesh of structure is very regular.

3.2 Characteristics of the mesh

the structure is modelled by a mesh made up of 1440 elements QUAD4 (see Appear 3.2-a).



Appear 3.2-a: mesh of structure

The mesh is very coarse to reduce the computing time. It is refined more in the zone of propagation of crack. In this zone the dimension of the elements is of $25 \times 25 \text{ mm}$. The largest element used has a dimension equalizes with $25 \times 100 \text{ mm}$.

3.3 Quantities tested and results

One tests the values of K_I and K_{II} for the two funds of crack after each propagation. To check if these values are correct, one uses a relative tolerance equal to 5% for the values of K_I . On the other hand, to check if the value of K_{II} is null, one uses an absolute tolerance (threshold value) related to the value of K_I : quest null K_{II} is considered if its value is lower than 1% of the value of K_I . Indeed, in this case one can neglect the value of K_{II} .

One tests the maximum value of K_I and K_{II} between the two funds of crack.

Propagation	K_I reference [$\text{Pa}\sqrt{\text{mm}}$]	Tolerance [%]
1	2.2997E+07	5.0
2	2.5878E+07	5.0
3	2.8894E+07	5.0

Propagation	max K_{II} [$Pa\sqrt{mm}$]	K_I reference [$Pa\sqrt{mm}$]	K_{II} threshold [$Pa\sqrt{mm}$]
1	7.4881E+03	2.2997E+07	2.2997E+05
2	1.0356E+04	2.5878E+07	2.5878E+05
3	1.3550E+04	2.8894E+07	2.8894E+05

3.4 Remarks

All the values tested are in the tolerances used. That means that method `UPWIND` and the calculates correctly at the same time the position of the two funds of crack level sets.

The error obtained on the values of K_I is almost null and the values of K_{II} are always about 0.1% of the values of K_I . The got results are thus very satisfactory.

4 Modelization B

4.1 Characteristic of the modelization

method `SIMPLEXE` is used by `PROPA_FISS` to solve the equations of propagation of crack. **No auxiliary grid** is used.

4.2 Characteristics of the mesh

One uses the same mesh as that of modelization A.

4.3 Grandeurs tested and results

One tests the values of K_I and K_{II} for the two funds of crack after each propagation. To check if these values are correct, one uses a relative tolerance equal to 5% for the values of K_I . On the other hand, to check if the value of K_{II} is null, one uses an absolute tolerance (threshold value) related to the value of K_I : it is considered that K_{II} is null if its value is lower than 1% of the value of K_I . Indeed, in this case one can neglect the value of K_{II} .

One tests the maximum value of K_I and K_{II} between the two funds of crack.

Propagation	max K_I [$Pa\sqrt{mm}$]	K_I reference [$Pa\sqrt{mm}$]	Tolerance [%]
1	2.2914E+07	2.2997E+07	5.0
2	2.5803E+07	2.5878E+07	5.0
3	2.8809E+07	2.8894E+07	5.0

Propagation	max K_{II} [$Pa\sqrt{mm}$]	K_I reference [$Pa\sqrt{mm}$]	K_{II} threshold [$Pa\sqrt{mm}$]
1	7.4881E+03	2.2997E+07	2.2997E+05
2	9.9867E+03	2.5878E+07	2.5878E+05
3	1.2353E+04	2.8894E+07	2.8894E+05

4.4 Remarks

All the values tested are in the tolerances used. That means that method `SIMPLEXE` and the calculates correctly at the same time the position of the two crack tips level sets.

The error obtained on the values of K_I is almost null and the values of K_{II} are always about 0.1% of the values of K_I . The got results are thus very satisfactory.

5 Modelization C

5.1 Characteristic of the modelization

method GEOMETRIQUE is used by PROPA_FISS to solve the equations of propagation of crack. No auxiliary grid is used.

5.2 Characteristics of the mesh

One uses the same mesh as that of modelization A.

5.3 Grandeurs testées et résultats

One tests the values of K_I and K_{II} for the two funds of crack after each propagation. To check if these values are correct, one uses a relative tolerance equal to 5% for the values of K_I . On the other hand, to check if the value of K_{II} is null, one uses an absolute tolerance (threshold value) related to the value of K_I : it is considered that K_{II} is null if its value is lower than 1% of the value of K_I . Indeed, in this case one can neglect the value of K_{II} .

One tests the maximum value of K_I and K_{II} between the two funds of crack.

Propagation	max K_I [Pa \sqrt{mm}]	K_I reference [Pa \sqrt{mm}]	Tolerance [%]
1	2.2914E+07	2.2997E+07	5.0
2	2.5803E+07	2.5878E+07	5.0
3	2.8809E+07	2.8894E+07	5.0

Propagation	max K_{II} [Pa \sqrt{mm}]	K_I reference [Pa \sqrt{mm}]	K_{II} threshold [Pa \sqrt{mm}]
1	7.4881E+03	2.2997E+07	2.2997E+05
2	4.1930E+03	2.5878E+07	2.5878E+05
3	5.1550E+03	2.8894E+07	2.8894E+05

5.4 Remarks

All the values tested are in the tolerances used. That means that method GEOMETRIQUE and the calculates correctly at the same time the position of the two crack tips level sets.

The error obtained on the values of K_I is almost null and the values of K_{II} are always about 0.1% of the values of K_I . The got results are thus very satisfactory.

6 Summary of the results

All the methods used (UPWIND, SIMPLEXE and GEOMETRIQUE) made it possible to calculate well the position of a crack formed by two funds and propagating in mode I . The factors of intensity of constrained were calculated correctly and the methods used calculate correctly the level sets with each propagation. The got results make it possible to validate the implementation of multi-cracking (case of only one crack with several funds) in operator PROPA_FISS.