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## CRACK01 - Validation of Wizard Analysis Ace of the modulus Aster of Salome-Meca

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### Summarized

This test makes it possible to validate the command file obtained thanks to Wizard (assistant) *Analysis Ace* of the modulus Aster of Salome-meca. One recalls that this Wizard allows a computation of the rate of refund and stress intensity factors in 2D, in axi-symmetry and 3D, from a sane mesh of a structure, by means of the method X-FEM and the level-sets as well as automatic refinement of mesh.

The case treated here is a circular crack plunged in a presumedly infinite medium, resulting from the sslv134 benchmark.

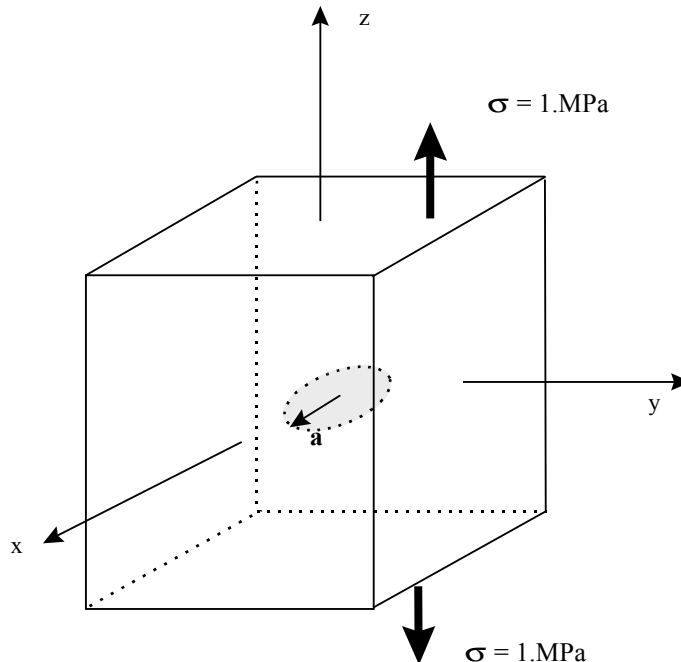
- The modelization A milked the problem in 3D (similar to the case test sslv134h),
- The modelization B milked the problem in 2D axisymmetric (similar to the case test sslv134i).

A each time, the value of the factor of intensity of the stresses in mode  $I$  is compared with the theoretical value resulting from an analytical solution.

## 1 Problem of reference

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### 1.1 Geometry



the crack is circular (*penny shaped ace*) of radius  $a$ , in the plane  $Oxy$ . So that the medium is regarded as infinite, the quantities characteristic of the solid mass are about 5 times higher than the radius  $a$ .

### 1.2 Material properties

Modulus Young:  $E = 2.10^5 MPa$

Poisson's ratio:  $\nu = 0.3$

Density:  $\rho = 7850 kg/m^3$

### 1.3 Boundary conditions and loadings

lower Face : uniform stress of tension  $\sigma_z = 1.MPa$

Upper face : uniform stress of tension  $\sigma_z = 1.MPa$

## 2 Reference solution

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### 2.1 Method of calculating used for the reference solution

For a circular crack of radius  $a$  in an infinite medium, subjected to a uniform tension  $\sigma$  according to the norm with the plane of the lips, local rate of energy restitution  $G(s)$  is independent of the curvilinear abscisse  $s$  and is worth [bib1]:

$$G(s) = \frac{(1-\nu^2)}{\pi E} 4\sigma^2 a$$

then the stress intensity coefficient  $K_I$  is given by the formula of Irwin:

$$G(s) = \frac{(1-\nu^2)}{E} K_I^2 \quad \text{that is to say} \quad K_I = \frac{2\sigma\sqrt{a}}{\sqrt{\pi}}$$

### 2.2 Results of reference

For the loading considered and  $a = 2m$ , one obtains:

$$G(s) = 11.586 J/m^2$$

$$K_I = 1,5958 MPa$$

### 2.3 Bibliographical references

- 1) Solution of Sneddon (1946) in G.C. Sih: Handbook of stress-intensity factors Institute of Fracture and Solid Mechanics - Lehigh University Bethlehem, Pennsylvania

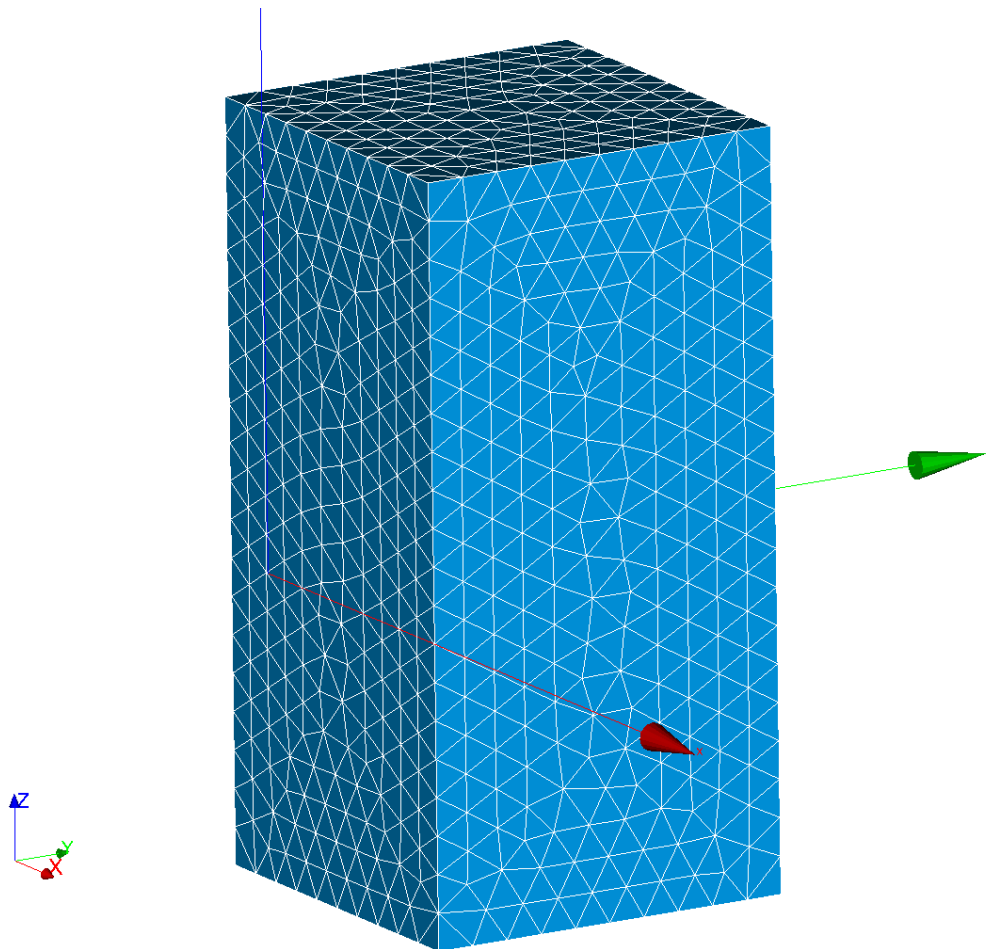
## 3 Modelization a: modelization in 3D

### 3.1 Characteristics of the modelization

the crack is not with a grid.  
A quarter of structure is modelled.  
Conditions of symmetry on the side sides will be applied.

### 3.2 Characteristics of the mesh

The mesh initial is healthy and relatively coarse. The initial size of meshes is of approximately  $h_0 = 1,25$  (unit of the mesh).



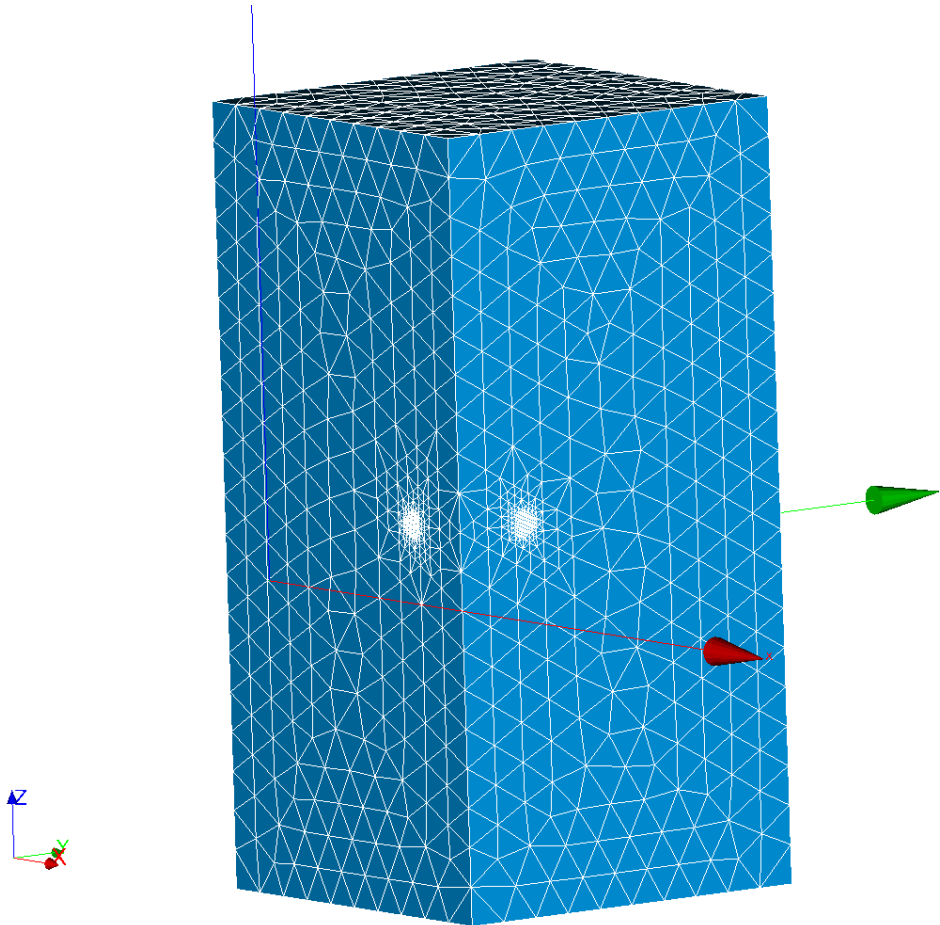
Appear 3.2-a: mesh initial 3D

Many nodes: 2927  
Number of meshes and type: 14086 TETRA4

This mesh will be refined in an automatic way before the mechanical resolution thanks to the software Homard in a zone around the crack tip. The target size of meshes of the refined mesh is  $h_c = 0,15$ . That implies 4 calls to Homard. After refinement, the size of meshes is of approximately  $h = 0,078$  and the mesh comprises:

Many nodes: 14228
Number of meshes and type: 79573 TETRA4

the radius of the refined zone east  $R_{ref} = 6h$ .



Appear 3.2-b: mesh 3D after refinement automatic

### 3.3 Quantities tested and results

One tests the value of  $K_I$  calculated by the command `CALC_G` along the crack tip. Theoretically,  $K_I$  is constant along the crack tip. It is thus checked that the max and the min of the values of  $K_I$  along the crack tip are close to the value of reference.

Integration contour is:  $2h - 5h$ .  
The lissage by default is used.

Standard	identification	Reference of reference	% tolerance
$max(K_I)$	1,595 106	ANALYTIQUE	3.0
$min(K_I)$	formulates 1,595	106	3.0

## 4 3,0 Modelization b: modelization in axi-symmetry

### 4.1 Characteristics of the modelization

the crack is not with a grid.  
Only one section of structure is modelled.

### 4.2 Characteristics of the mesh

The mesh initial is healthy and relatively coarse. The initial size of meshes is of approximately  $h_0 = 1,25$  (unit of the mesh).

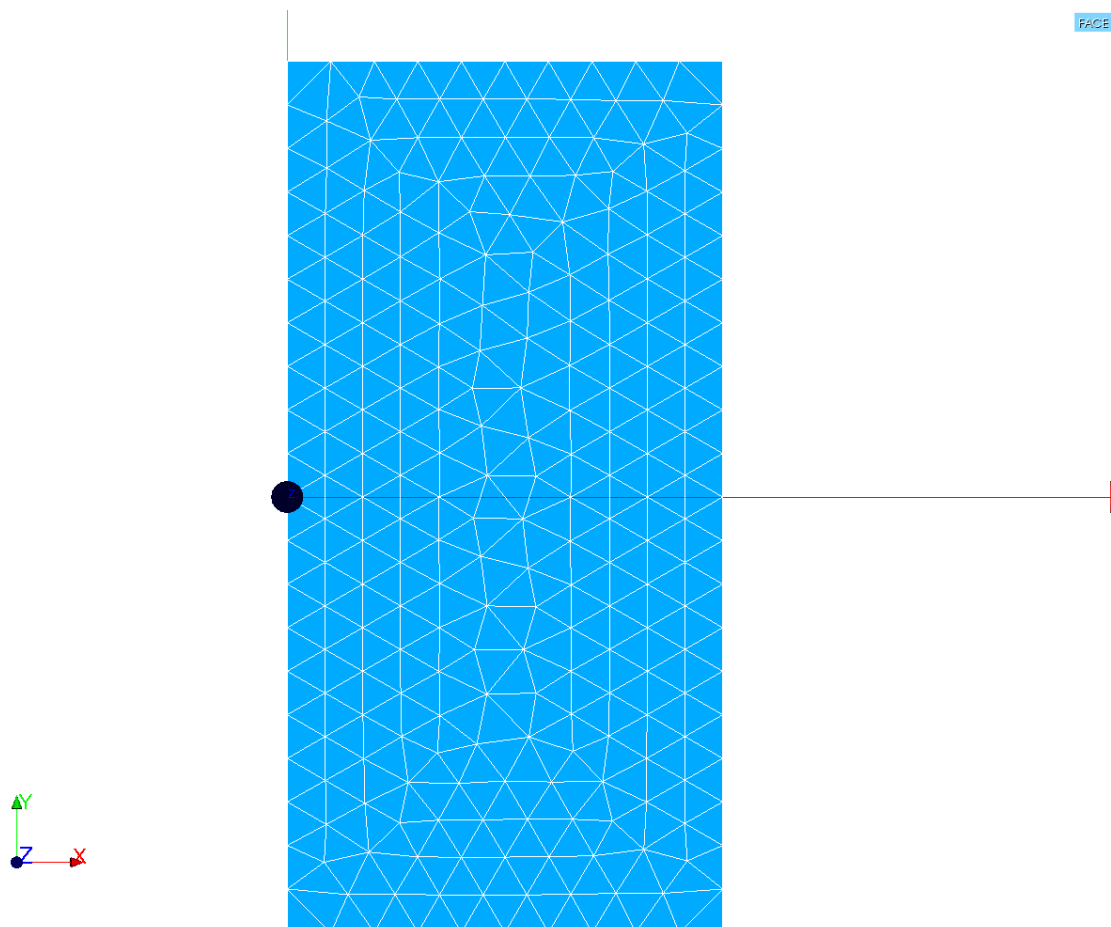


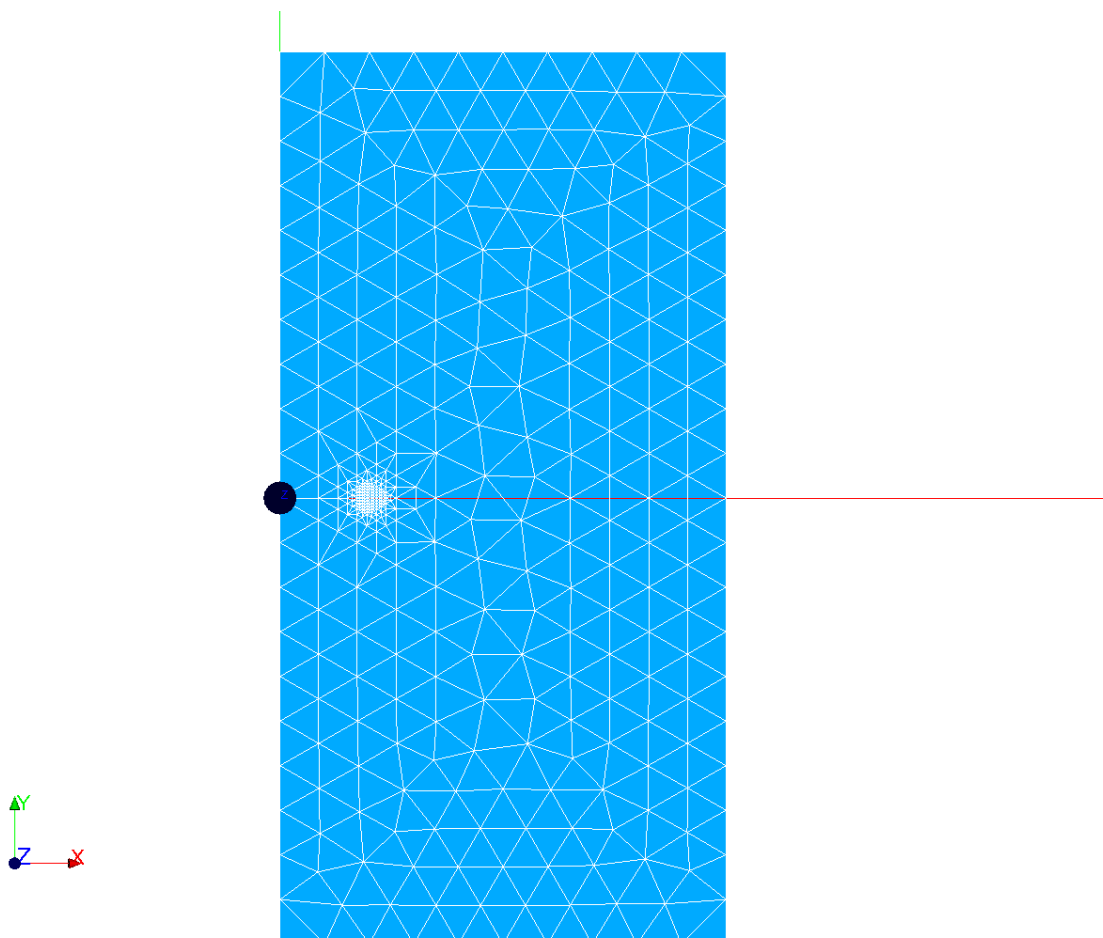
Figure 4.2-a : 4.2-a axisymmetric mesh 2d initial

Number of nodes: 251  
Number of meshes and type: 440 TRIA3

This mesh will be refined in an automatic way before the mechanical resolution thanks to the software Homard in a zone around the crack tip. The target size of meshes of the refined mesh is  $h_c = 0,15$ . That implies 4 calls to Homard. After refinement, the size of meshes is of approximately  $h = 0,078$  and the mesh comprises:

Many nodes: 425  
Number of meshes and type: 788 TRIA3  
the radius of the refined zone east  $R_{raff} = 6h$ .

Warning : The translation process used on this website is a "Machine Translation". It may be imprecise and inaccurate in whole or in part and is provided as a convenience.



Appear 4.2-b: axisymmetric mesh 2d after automatic refinement

## 4.3 Quantities tested and results

One tests the values of  $G$  and  $K_I$  calculated `CALC_G` by the command.

Integration contour is: 2h – 5h.

Standard	identification	Reference of reference	% tolerance
$G$	11,58	ANALYTIQUE	3.0
$K_I$	1,595 106	ANALYTIQUE	3.0

## 5 Summaries of the results

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This test shows that the file of Aster commands obtained thanks to Wizard (assistant) *Ace-Analysis* of the modulus Aster of Salome-meca makes it possible to conclude a computation of crack harmfulness in 3D and 2D axisymmetric because the got results (rate of energy restitution and stress intensity factor) are in accordance with the analytical solution.